Time Series Analysis in AFNI

Outline: 6+ Hours of Edification

- Philosophy
- Sample FMRI data
- Theory underlying FMRI analyses: the HRF
- "Simple" or "Fixed Shape" regression analysis
 - ★ Theory and Hands-on examples
- "Deconvolution" or "Variable Shape" analysis
 - ★ Theory and Hands-on examples
- Advanced Topics

Goals: Conceptual Understanding + Prepare to Try It Yourself

Data Analysis Philosophy

- <u>Signal</u> = Measurable response to stimulus
- Noise = Components of measurement that interfere with detection of signal
- Statistical detection theory:
 - ★ Understand relationship between stimulus & signal
 - ★ Characterize noise statistically
 - ★ Can then devise methods to distinguish noise-only measurements from signal+noise measurements, and assess the methods' reliability
 - ★ Methods and usefulness depend strongly on the assumptions
 - Some methods are "robust" against erroneous assumptions, and some are not

FMRI Philosopy: Signals and Noise

- FMRI <u>Stimulus→Signal</u> connection and <u>noise</u> <u>statistics</u> are both poorly characterized
- Result: there is no "best" way to analyze FMRI time series data: there are only "reasonable" analysis methods
- To deal with data, must make some assumptions about the signal and noise
- Assumptions will be wrong, but must do something
- Different kinds of experiments require different kinds of analyses
 - ★ Since signal models and questions you ask about the signal will vary
 - ★ It is important to understand what is going on, so you can select and evaluate "reasonable" analyses

Meta-method for creating analysis methods

- Write down a mathematical model connecting stimulus (or "activation") to signal
- Write down a statistical model for the noise
- Combine them to produce an equation for measurements given signal+noise
 - ★ Equation will have unknown parameters, which are to be estimated from the data
 - ★ N.B.: signal may have zero strength
- Use statistical detection theory to produce an algorithm for processing the measurements to assess signal presence and characteristics
 - ★ e.g., least squares fit of model parameters to data

Time Series Analysis on Voxel Data

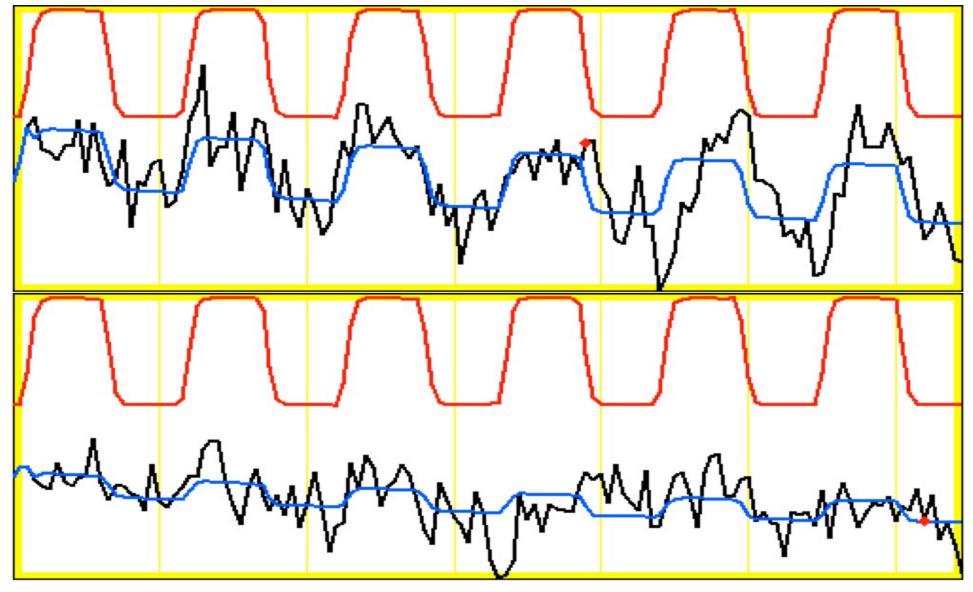
- Most common forms of FMRI analysis involve fitting an activation+BOLD model to each voxel's time series *separately* (AKA "univariate" analysis)
 - ★ Some pre-processing steps may do inter-voxel computations
 - e.g., spatial smoothing to reduce noise
- Result of model fits is a set of parameters at each voxel, estimated from that voxel's data
 - ★ e.g., activation amplitude, delay, shape
 - ★ "SPM" = statistical parametric map
- Further analysis steps operate on individual SPMs
 - ★ e.g., combining/contrasting data among subjects

Some Sample FMRI Data Time Series

- First: Block-trial FMRI data
 - ★ "Activation" occurs over a sustained period of time (say, 10 s or longer), usually from more than one stimulation event, in rapid succession
 - ★ BOLD (hemodynamic) response accumulates from multiple close activations and is large
 - ★ BOLD response is often visible in time series
- Next 5 slides: same brain voxel in 9 imaging runs
 - ★ black curve (noisy) = data
 - ★ red curve (above data) = ideal model response
 - ★ blue curve (within data) = model fitted to data
 - ★ somatosensory task (finger being rubbed)

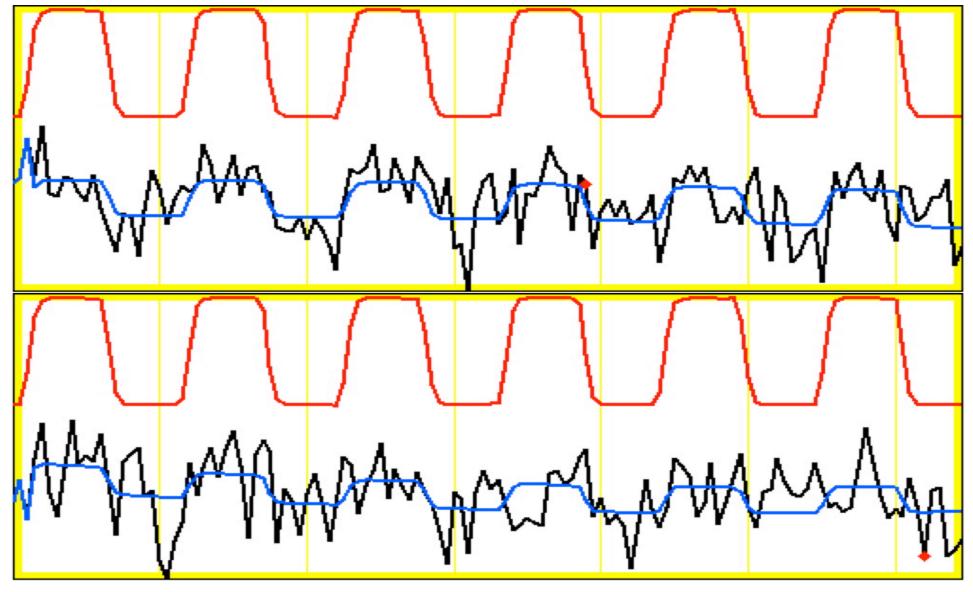
Block-trials: 27 s "on" / 27 s "off"; TR=2.5 s; 130 time points/run

Same Voxel: Runs 3 and 4



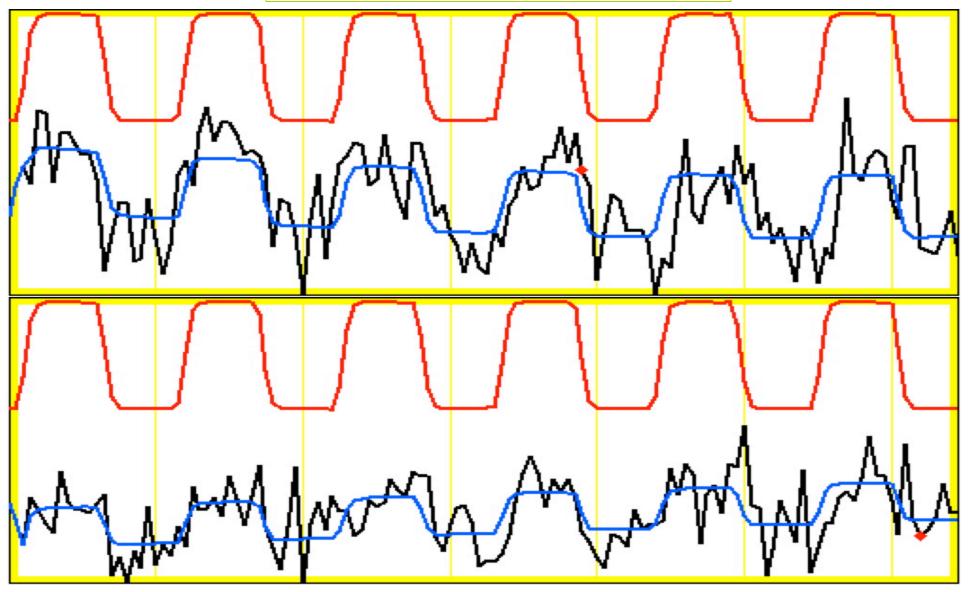
Block-trials: 27 s "on" / 27 s "off"; TR=2.5 s; 130 time points/run

Same Voxel: Runs 5 and 6



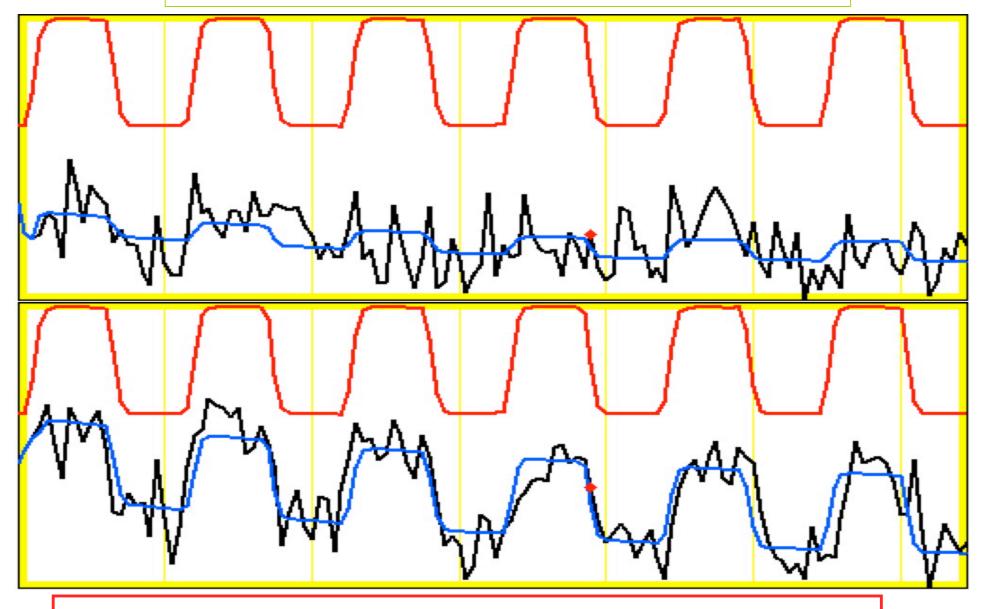
Block-trials: 27 s "on" / 27 s "off"; TR=2.5 s; 130 time points/run

Same Voxel: Runs 7 and 8



Block-trials: 27 s "on" / 27 s "off"; TR=2.5 s; 130 time points/run

Same Voxel: Run 9 and Average of all 9

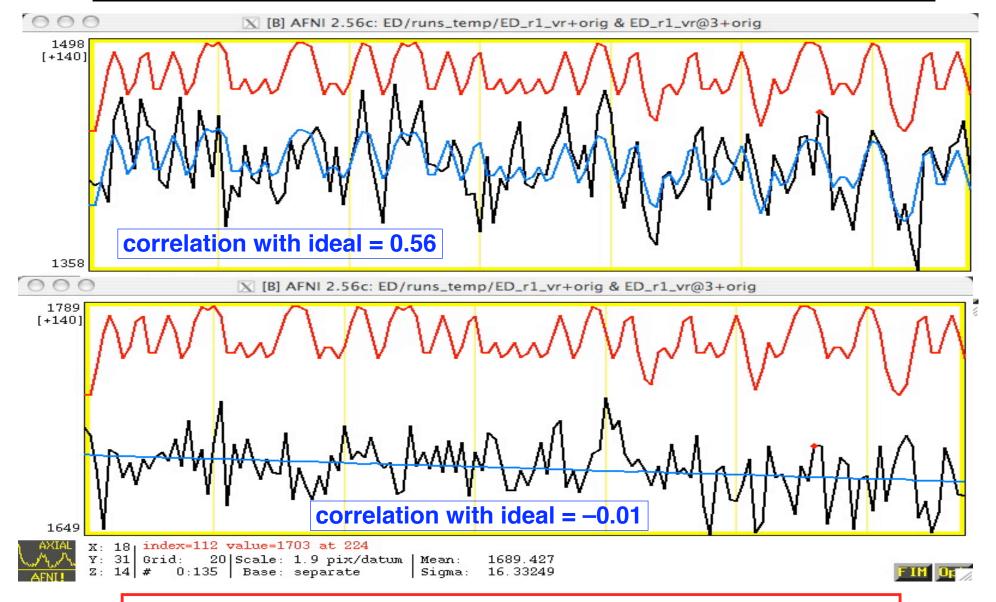


⇒ Activation amplitude and shape are variable! Why???

More Sample FMRI Data Time Series

- Second: Event-related FMRI
 - ★ "Activation" occurs in single relatively brief intervals
 - ★ "Events" can be randomly or regularly spaced in time
 - If events are randomly spaced in time, signal model itself <u>looks</u> noise-like (to the human eye)
 - ★ BOLD response to stimulus tends to be weaker since fewer nearby-in-time "activations" have overlapping hemodynamic responses
- Next slide: Visual stimulation experiment

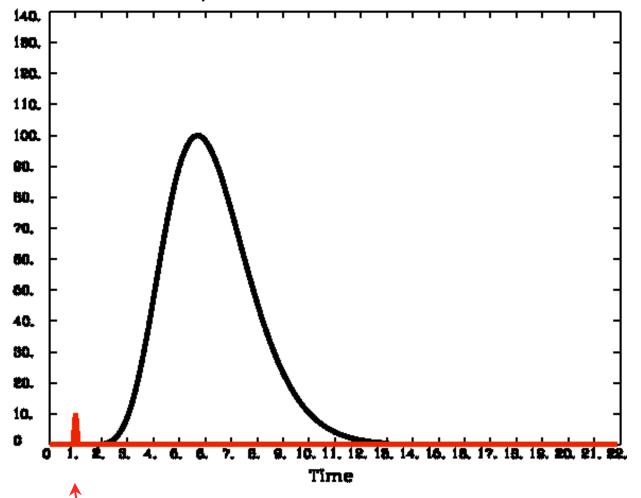
Two Voxel Time Series from Same Run



Lesson: ER-FMRI activation is not obvious via casual inspection

Hemodynamic Response Function (HRF)

 HRF is the idealization of measurable FMRI signal change responding to a single activation cycle (up and down) from a stimulus in a voxel



Response to brief activation (< 1 s):

- delay of 1-2 s
- rise time of 4-5 s
- fall time of 4-6 s
- model equation:

$$h(t) \propto t^b e^{-t/c}$$

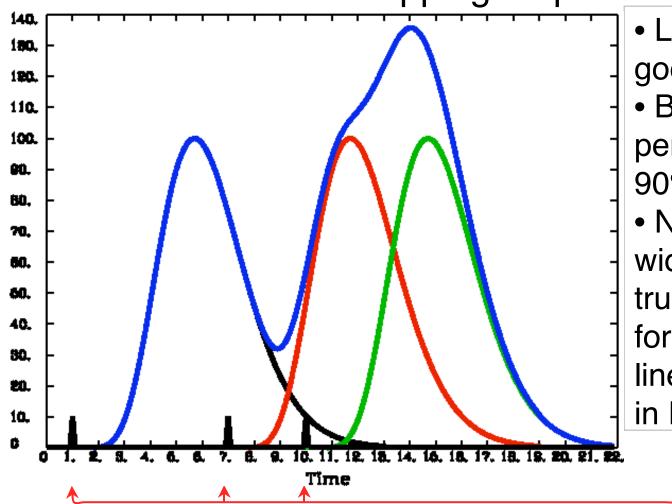
h(t) is signal change t seconds
 after activation

1 Brief Activation

Linearity of HRF

 Multiple activation cycles in a voxel, closer in time than duration of HRF:

★ Assume that overlapping responses add

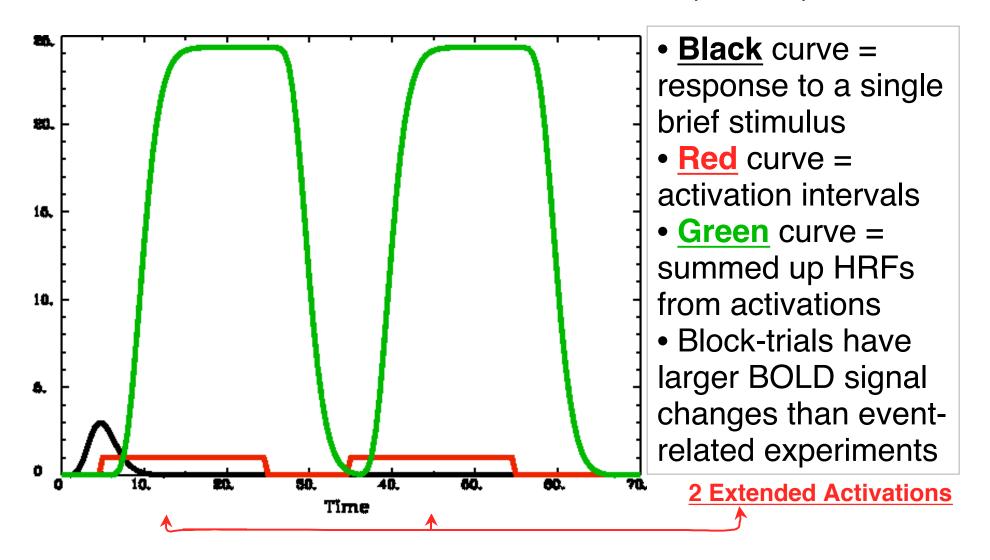


- Linearity is a pretty good assumption
- But not apparently perfect about
 90% correct
- Nevertheless, is widely taken to be true and is the basis for the "general linear model" (GLM) in FMRI

3 Brief Activations

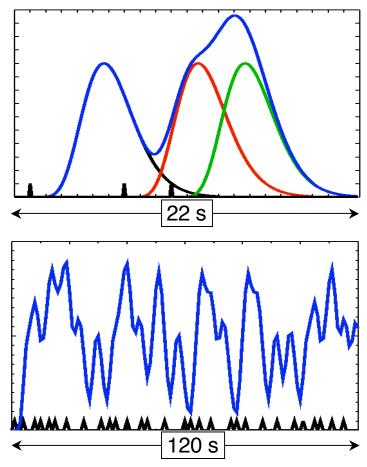
Linearity and Extended Activation

- Extended activation, as in a block-trial experiment:
 - ★ HRF accumulates over its duration (≈ 10 s)



Convolution Signal Model

- FMRI signal we look for in each voxel is taken to be sum of the individual trial HRFs
 - ★ Stimulus timing is assumed known (or measured)
 - ★ Resulting time series (blue curves) are called the convolution of the HRF with the stimulus timing
- Must also allow for baseline and baseline drifting
 - ★ Convolution models only the FMRI signal changes

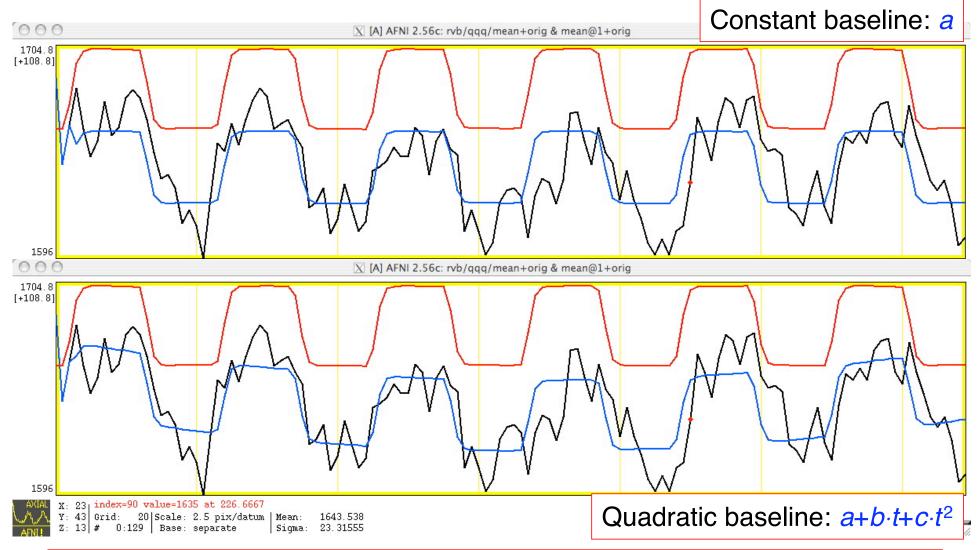


 Real data starts at and returns to a nonzero, slowly drifting baseline

Simple Regression Models

- Assume a fixed shape h(t) for the HRF
 - \star e.g., $h(t) = t^{8.6} \exp(-t/0.547)$ [MS Cohen, 1997]
 - ★ Convolved with stimulus timing (e.g., AFNI program waver), get ideal response function r(t)
- Assume a form for the baseline
 - \star e.g., $a + b \cdot t$ for a constant plus a linear trend
- In each voxel, fit data Z(t) to a curve of the form $Z(t) \approx a + b \cdot t + \beta \cdot r(t)$
 - a, b, β are unknown parameters to be calculated in each voxel
 - a,b are "nuisance" parameters
 - β is amplitude of r(t) in data = "how much" BOLD

Simple Regression: Example



 Necessary baseline model complexity depends on duration of continuous imaging — e.g., 1 parameter per 100 seconds

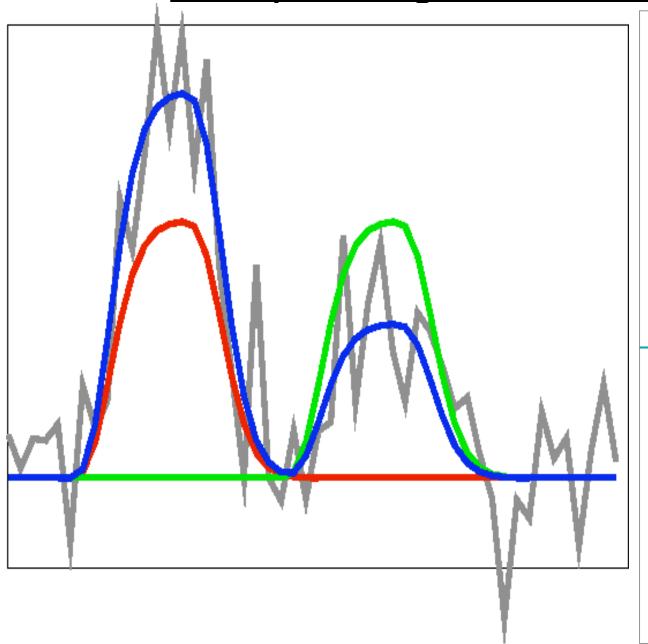
<u>Multiple Stimuli = Multiple Regressors</u>

- Usually have more than one class of stimulus or activation in an experiment
 - ★ e.g., want to see size of "face activation" vis-à-vis "house activation"; or, "what" vs. "where" activity
- Need to model each separate class of stimulus with a separate response function $r_1(t)$, $r_2(t)$, $r_3(t)$,
 - \star Each $r_j(t)$ is based on the stimulus timing for activity in class number j
 - ★ Calculate a β_j amplitude = amount of $r_j(t)$ in voxel data time series Z(t)
 - ★ Contrast \(\beta \)s to see which voxels have differential activation levels under different stimulus conditions
 - o e.g., statistical test on the question $\beta_1 \beta_2 = 0$?

Multiple Stimuli - Important Caveat

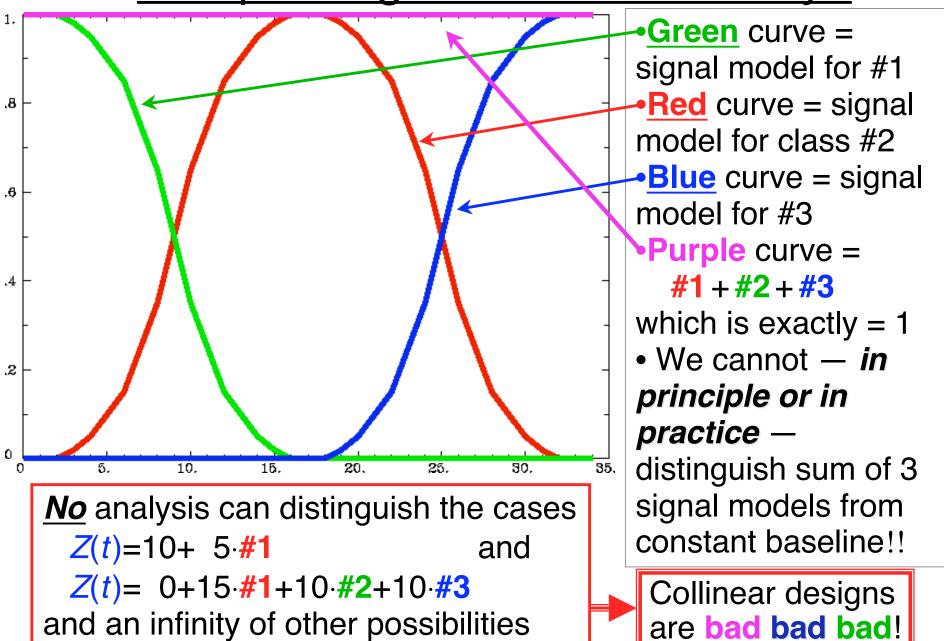
- You do <u>not</u> model the baseline condition
 - e.g., "rest", visual fixation, high-low tone discrimination, or some other simple task
- FMRI can only measure <u>changes</u> in MR signal levels between tasks
 - So you need some simple-ish task to serve as a reference point
- The baseline model (e.g., $a + b \cdot t$) takes care of the signal level to which the MR signal returns when the "active" tasks are turned off
 - Modeling the reference task explicitly would be redundant (or "collinear", to anticipate a forthcoming jargon word)

Multiple Regressors: Cartoon

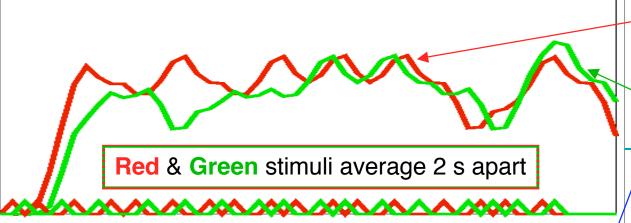


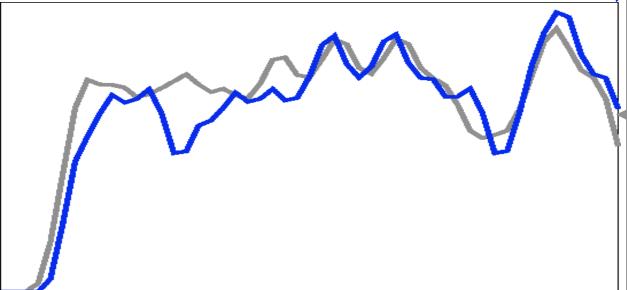
- Red curve = signal model for class #1
- Green curve = signal model for #2
- Blue curve = $\beta_1 \cdot \#1 + \beta_2 \cdot \#2$ where β_1 and β_2 vary from 0.1 to 1.7 in the animation
- Goal of regression is to find β_1 and β_2 that make the blue curve best fit the data time series
- Gray curve = 1.5.#1+0.6.#2+noise
- = simulated data

Multiple Regressors: Collinearity!!



Multiple Regressors: Near Collinearity





Stimuli are too close in time to distinguish response #1 from #2, considering noise

- Red curve = signal model for class #1
- Green curve = signal model for #2
- Blue curve =

 $\beta_1 \cdot \#1 + (1 - \beta_1) \cdot \#2$

where β_1 varies randomly from 0.0 to 1.0 in animation

•Gray curve =

 $0.66 \cdot #1 + 0.33 \cdot #2$

- = simulated data with no noise
- Lots of different combinations of #1 and #2 are decent fits to gray curve

Equations: Notation

- Will generally follow notation of Doug Ward's manual for the AFNI program 3dDeconvolve
- Time: continuous in reality, but in steps in the data
 - \star Functions of continuous time are written like f(t)
 - * Functions of discrete time expressed like $f(\underline{n} \cdot \underline{TR})$ where n=0,1,2,... and TR=time step
 - \star Usually use subscript notion f_n as shorthand
 - * Collection of numbers assembled in a column is a

$$\begin{cases} \text{vector of} \\ \text{length } N \end{cases} = \begin{bmatrix} f_0 \\ f_1 \\ f_2 \\ \vdots \\ f_{N-1} \end{bmatrix} = \mathbf{f} \quad \begin{bmatrix} A_{00} & A_{01} & \cdots & A_{0,N-1} \\ A_{10} & A_{11} & \cdots & A_{1,N-1} \\ \vdots & \vdots & \ddots & \vdots \\ A_{M-1,0} & A_{M-1,1} & \cdots & A_{M-1,N-1} \end{bmatrix} = \mathbf{A} = \{M \times N \text{ matrix}\}$$

Equations: Single Response Function

- In each voxel, fit data Z_n to a curve of the form
 - $Z_n \approx a + b \cdot t_n + \beta \cdot r_n$ for n=0,1,...,N-1 (N=# time pts)
 - a, b, β are unknown parameters to be calculated in each voxel
 - a,b are "nuisance" baseline parameters
 - β is amplitude of r(t) in data = "how much" BOLD
 - Baseline model might be more complicated for long (> 150 s) continuous imaging runs:
 - $150 < T < 300 \text{ s: } a+b\cdot t+c\cdot t^2$
 - Longer: $a+b\cdot t+c\cdot t^2+\lceil T/200\rceil$ low frequency components
 - Might also include as extra baseline components the estimated subject head movement time series, in order to remove residual contamination from such artifacts

Equations: Multiple Response Functions

• In each voxel, fit data Z_n to a curve of the form

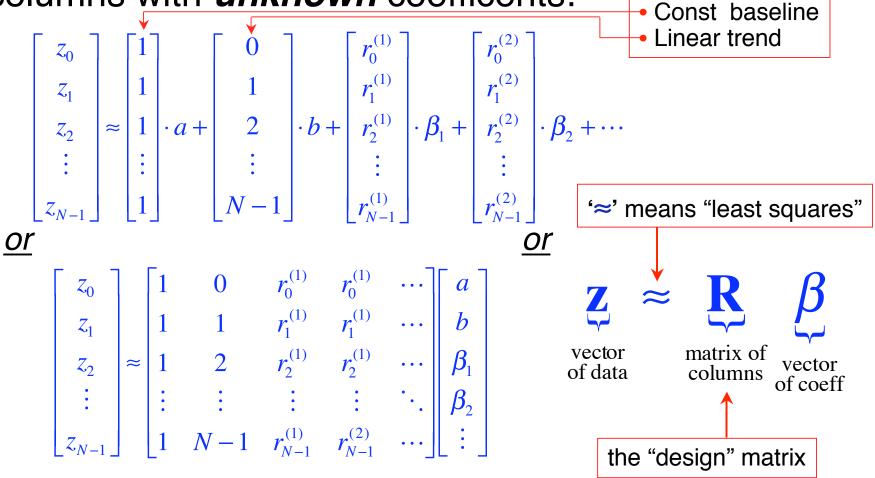
$$Z_n \approx [\text{baseline}]_n + \beta_1 \cdot r_n^{(1)} + \beta_2 \cdot r_n^{(2)} + \beta_3 \cdot r_n^{(3)} + \cdots$$

- β_j is amplitude in data of $r_n^{(j)} = r_j(t_n)$; i.e., "how much" of j^{th} response function in the data time series
- In simple regression, each $r_j(t)$ is derived directly from stimulus timing **and** user-chosen HRF model
 - In terms of stimulus times: $r_n^{(j)} = \sum_{k=1}^{K_j} h(t_n \tau_k^{(j)})$
- If stimulus occurs on the imaging TR time-grid, stimulus can be represented as a 0-1 time series: $\begin{bmatrix} s_0^{(j)} & s_1^{(j)} & s_2^{(j)} & s_3^{(j)} & \cdots \end{bmatrix}$ where $s_k^{(j)}=1$ if stimulus $\#_j$ is on at time $t=k\cdot TR$, and $s_k^{(j)}=0$ if $\#_j$ is off at that time:

$$r_n^{(j)} = h_0 s_n^{(j)} + h_1 s_{n-1}^{(j)} + h_2 s_{n-2}^{(j)} + h_3 s_{n-3}^{(j)} + \dots = \sum_{q=0}^{p} h_q s_{n-q}^{(j)}$$

Equations: Matrix-Vector Form

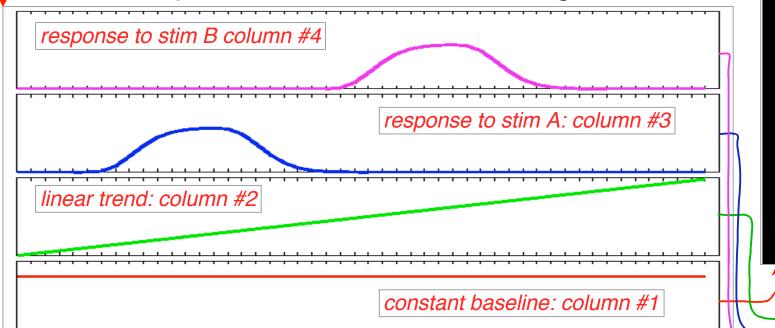
Express known data vector as a sum of known columns with unknown coefficents:



z depends on the voxel; R doesn't

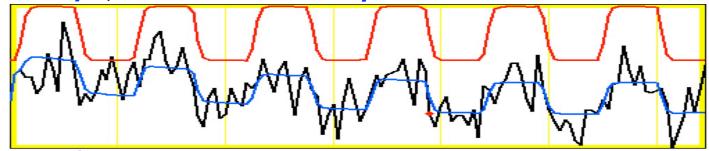
Visualizing the R Matrix

- Can graph columns, as shown below
 - But might have 20-50 columns
- Can plot columns on a grayscale, as shown at right
 - Easier to show many columns
 - In this plot, darker bars means larger numbers



Solving $z \approx R\beta$ for β

- Number of equations = number of time points
 - ★ 100s per run, but perhaps 1000s per subject
- Number of unknowns usually in range 5–50
- Least squares solution: $\hat{\beta} = [\mathbf{R}^T \mathbf{R}]^{-1} \mathbf{R}^T \mathbf{z}$
 - \star $\hat{\beta}$ denotes an *estimate* of the true (unknown) β
 - \star From $\hat{\beta}$, calculate $\hat{z} = R\hat{\beta}$ as the *fitted model*



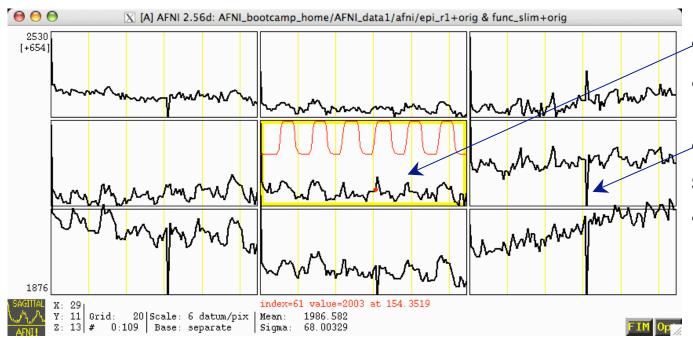
- o $\mathbf{Z} \hat{\mathbf{Z}}$ is the **residual time series** = noise (we hope)
- Collinearity: when matrix R^TR can't be inverted
 - ★ Near collinearity: when inverse exists but is huge

Simple Regression: Recapitulation

- Choose HRF model h(t) [AKA fixed-model regression]
- Build model responses r_n(t) to each stimulus class
 Using h(t) and the stimulus timing
- Choose baseline model time series
 - ★ Constant + linear + quadratic + movement?
- Assemble model and baseline time series into the columns of the R matrix
- For each voxel time series z, solve $z \approx R\beta$ for β
- Individual subject maps: Test the coefficients in $\hat{\beta}$ that you care about for statistical significance
- **Group maps**: Transform the coefficients in $\hat{\beta}$ that you care about to Talairach space, and perform statistics on these $\hat{\beta}$ values

Sample Data Analysis: Simple Regression

- Enough theory (for now: more to come later!)
- To look at the data: type cd AFNI data1/afni; then afni
- Switch Underlay to dataset epi r1
 - ★ Then Sagittal Image and Graph
 - * FIM-Pick Ideal; then click afni/ideal r1.1D; then Set
 - * Right-click in image, Jump to (ijk), then 29 11 13, then Set



- Data clearly has activity in sync with reference
- Data also has a big spike, which is annoying
 - Subject head movement!

Preparing Data for Analysis

- Six preparatory steps are possible:
 - ★ Image registration (realignment): program <u>3dvolreg</u>
 - ★ Image smoothing: program <u>3dmerge</u>
 - ★ Image masking: program 3dClipLevel or 3dAutomask
 - ★ Conversion to percentile: programs 3dTstat and 3dcalc
 - ★ Censoring out time points that are bad: program 3dToutcount or 3dTqual
 - ★ Catenating multiple imaging runs into 1 big dataset: program <u>3dTcat</u>
- Not all steps are necessary or desirable in any given case
- In this first example, will only do registration, since the data obviously needs this correction

Data Analysis Script

• In file epi_r1_decon:

-fitts epi r1 fitts

```
    waver creates model time series

waver -GAM
      -input epi r1 stim.1D
                                   from input stimulus timing in file
      -TR 2.5
                                    epi r1 stim.1D
     > epi r1 ideal.1D

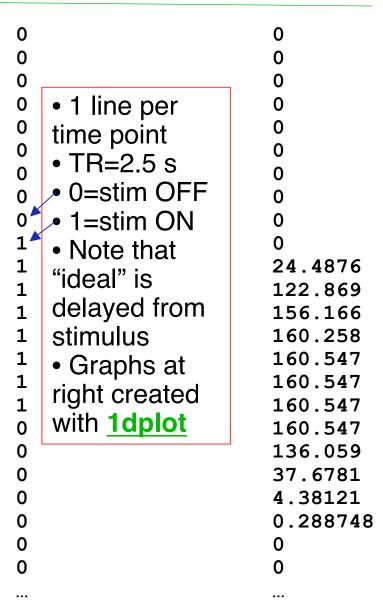
    Plot a 1D file to screen with

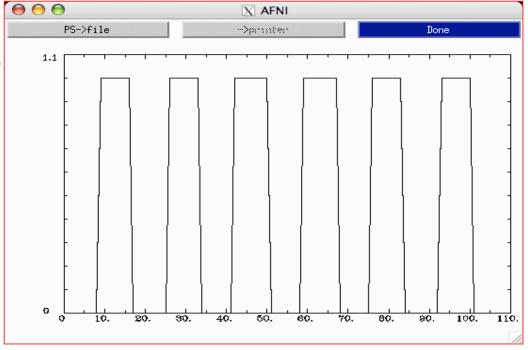
                                       1dplot epi r1 ideal.1D
3dvolreg -base 2
                                   3dvolreg (3D image registration)
        -prefix epi r1 reg
        -1Dfile epi r1 mot.1D
                                    will be covered in a later presentation
        -verb
        epi r1+orig
                                   • 3dDeconvolve = regression code
3dDeconvolve
    -input epi r1 reg+orig
                                 \ 	→ Name of input dataset
    -nfirst
               2
                                 \ 		 Index of first sub-brick to process
    -num stimts 1
                                 -stim file 1 epi r1 ideal.1D \ ← Name of first input model time series file
                                 -stim label 1 AllStim
                                 \ \leftarrow Indicates to output t-statistic for \beta weights
    -tout
                                 -bucket epi r1 func
```

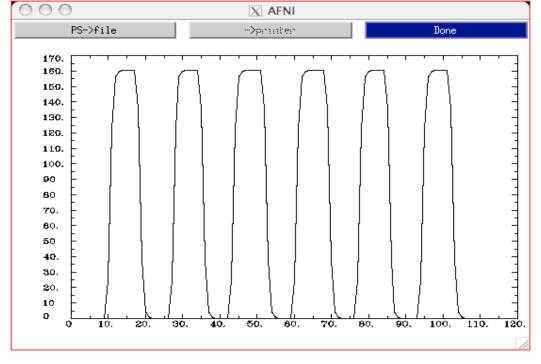
◆ Name of output model fit dataset

Contents of 1D files

epi_r1_stim.1D epi_r1_ideal.1D







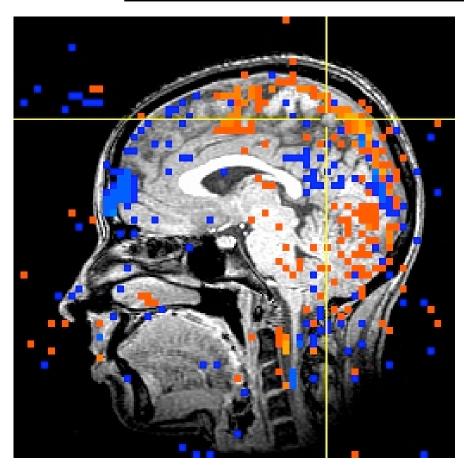
To Run Script and View Results

- type source epi_r1_decon; then wait for programs to run
- type afni to view what we've got
 - ★ Switch Underlay to epi_r1_reg (output from 3dvolreg)
 - * Switch Overlay to epi_r1_func (output from 3dDeconvolve)
 - ★ Sagittal Image and Graph viewers
 - * FIM→Ignore→2 to have graph viewer not plot 1st 2 time pts
 - ★ FIM→Pick Ideal; pick epi_r1_ideal.1D (output from waver)
- Define Overlay to set up functional coloring
 - Olay \rightarrow Allstim[0] Coef (sets coloring to be from model fit β)
 - Thr→Allstim[0] t-s (sets threshold to be model fit t-statistic)
 - See Overlay (otherwise won't see the function!)
 - Play with threshold slider to get a meaningful activation map (e.g., t=4 is a decent threshold)

More Viewing the Results

- Graph viewer: Opt→Tran 1D→Dataset #N to plot the model fit dataset output by 3dDeconvolve
 - Will open the control panel for the Dataset #N plugin
 - Click first Input on; then choose Dataset epi_r1_fitts+orig
 - Also choose Color dk-blue to get a pleasing plot
 - Then click on Set+Close (to close the plugin panel)
 - Should now see fitted time series in the graph viewer instead of data time series
 - Graph viewer: click Opt→Double Plot→Overlay on to make the fitted time series appear as an overlay curve
 - This tool lets you visualize the quality of the data fit
- Can also now overlay function on MP-RAGE anatomical by using Switch Underlay to anat+orig dataset
 - Probably won't want to graph the anat+orig dataset!

Stimulus Correlated Movement?



- 3dvolreg saved the motion parameters estimates into file epi_r1_mot.1D
- For fun: 1dplot epi_r1_mot.1D

- Extensive "activation" (i.e., correlation of data time series with model time series) along the top of the brain is an indicator of stimulus correlated motion artifact
- Can remain even after registration, due to errors in registration, magnetic field inhomogeneities, etc.
- Can be partially removed by using the estimated movement history (from 3dvolreg) as additional baseline model functions

Removing Residual Motion Artifacts

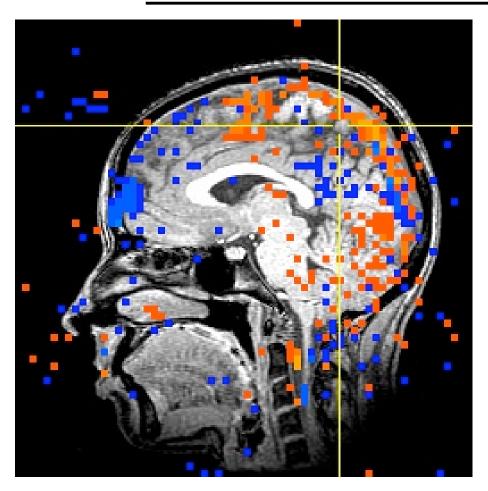
Last part of script epi_r1_decon:

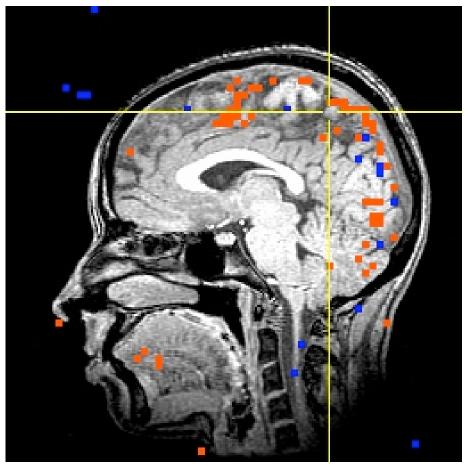
```
3dDeconvolve
    -input epi r1 reg+orig
    -nfirst
    -num stimts 7
    -stim file 1 epi r1 ideal.1D
   -stim label 1 AllStim
    -stim file 2 epi r1 mot.1D'[0]'
    -stim base
    -stim file
                3 epi r1 mot.1D'[1]'
    -stim base
                4 epi r1 mot.1D'[2]'
    -stim file
    -stim base
    -stim file 5 epi r1 mot.1D'[3]'
    -stim base
    -stim file
                6 epi r1 mot.1D'[4]'
   -stim base
    -stim file
                7 epi r1 mot.1D'[5]'
    -stim base
    -tout
    -bucket epi r1 func mot
    -fitts epi r1 fitts mot
```

These new lines add 6 regressors to the model and assign them to the baseline (-stim_base option)

Output files: take a moment to look at results

Some Results: Before and After





No: movement parameters are not in baseline model

Yes: movement parameters are in baseline model

t-statistic threshold set to a p-value of 10⁻⁴ in both images

Multiple Stimulus Classes

- The experiment analyzed here in fact is more complicated
 - ★ There are 4 related visual stimulus types
 - ★ One goal is to find areas that are differentially activated between these different types of stimuli
 - ★ We have 4 imaging runs, 108 useful time points each (skipping first 2 in each run) that we will analyze together
 - Already registered and put together into dataset rall_vr+orig
 - ★ Stimulus timing files are in subdirectory stim_files/
 - ★ Script file waver_ht2 will create HRF models for regression:

```
cd stim_files
waver -dt 2.5 -GAM -input scan1to4a.1D > scan1to4a_hrf.1D
waver -dt 2.5 -GAM -input scan1to4t.1D > scan1to4t_hrf.1D
waver -dt 2.5 -GAM -input scan1to4h.1D > scan1to4h_hrf.1D
waver -dt 2.5 -GAM -input scan1to4l.1D > scan1to4l_hrf.1D
cd ...
```

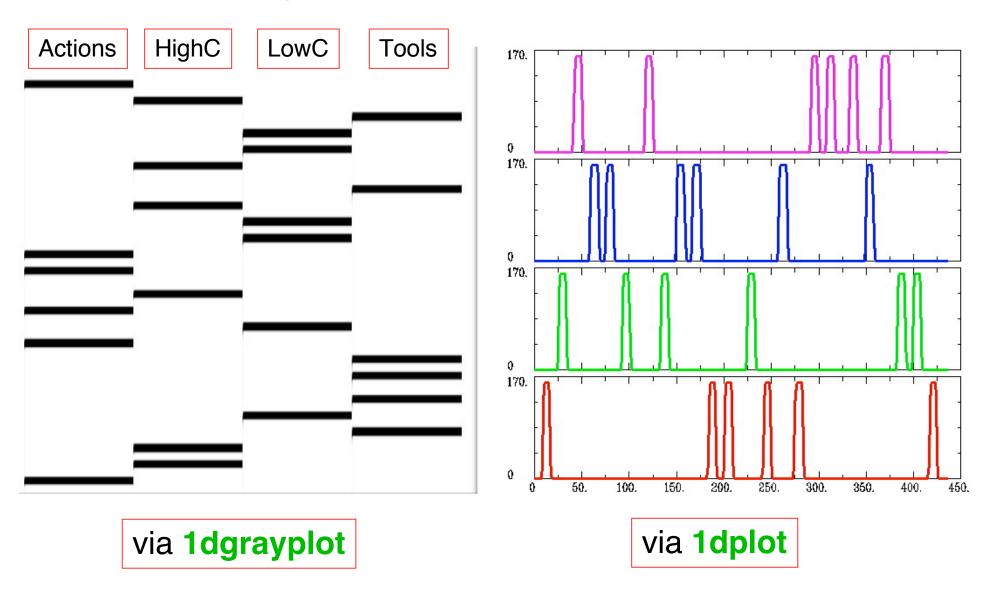
- ★ Type source waver_ht2 to run this script
 - Might also use 1dplot to check if things are reasonable

Regression with Multiple Model Files

Script file decon_ht2 does the job:

- Run this script by typing source decon_ht2 (takes a few minutes)
 - Stim #1 = visual presentation of active movements
 - Stim #2 = visual presentation of simple (tool-like) movements
 - Stims #3 and #4 = high and low contrast gratings

Regressors for This Script



0 -concat contrasts/runs.1D = file that indicates where 108 216 new imaging runs start 324

- -full first
- -fout -tout

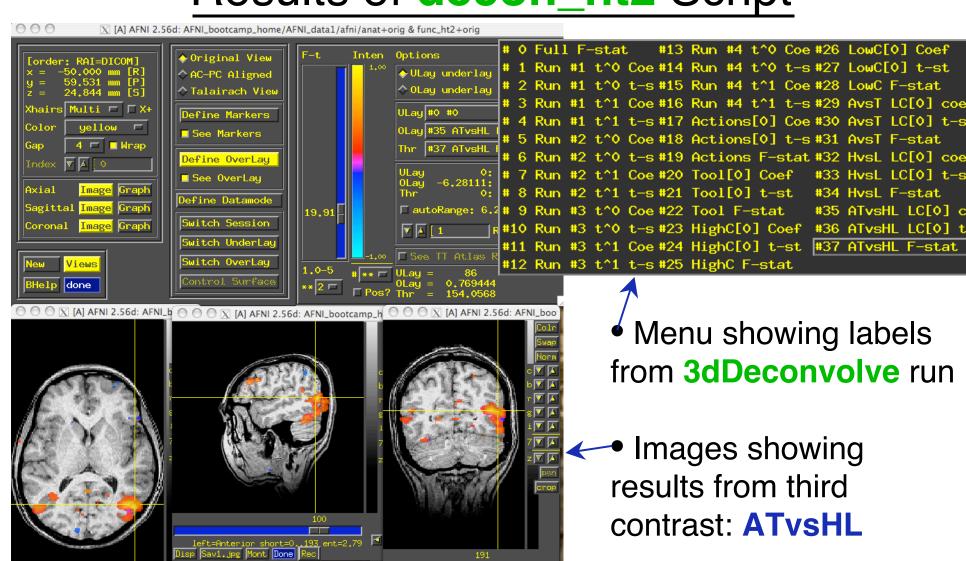
- = put **full model** statistic first in output file, not last
- = output both *F* and *t*-statistics
- The full model statistic is an F-statistic that shows how well the sum of all 4 input model time series fits voxel time series data
- The individual models also will get individual *F* and *t*-statistics indicating the significance of their individual contributions to the time series fit
 - \star i.e., F_{Actions} tells if model (Actions+HighC+LowC+Tools+baseline) explains more of the data variability than model (HighC+LowC+Tools+baseline)

```
-glt 1 contrasts/contr_AvsT.txt -glt_label 1 AvsT
-glt 1 contrasts/contr_HvsL.txt -glt_label 2 HvsL
-glt 1 contrasts/contr_ATvsHL.txt -glt_label 3 ATvsHL
```

- GLTs are General Linear Tests
- 3dDeconvolve provides tests for each regressor separately, but if you want to test combinations or contrasts of the β weights in each voxel, you need the -glt option
- File contrasts/contr_AvsT.txt = 00000001-100 (one line with 12 numbers)
- Goal is to test a linear combination of the β weights
 - * In this data, we have 12 β weights: 8 baseline parameters (2 per imaging run), which are first in the β vector, and 4 regressor magnitudes, which are from -stim file options
 - \star This particular test contrasts the Actions and Tool β s
 - tests if $\beta_{\text{Actions}} \beta_{\text{Tool}} \neq 0$

- File contrasts/contr_HvsL.txt = 0000000001-1
 - Goal is to test if $\beta_{\text{HighC}} \beta_{\text{LowC}} \neq 0$
- File contrasts/contr_ATvsHL.txt = 0000000011-1-1
 - Goal is to test if $(\beta_{Actions} + \beta_{Tool}) (\beta_{HighC} + \beta_{LowC}) \neq 0$
 - Regions where this statistic is significant will have had different amounts of BOLD signal change in the activity viewing tasks versus the grating viewing tasks
 - This is a way to factor out primary visual cortex
- -glt_label 3 ATvsHL option is used to attach a meaningful label to the resulting statistics sub-bricks

Results of decon_ht2 Script



 Play with this yourself to get a feel for it

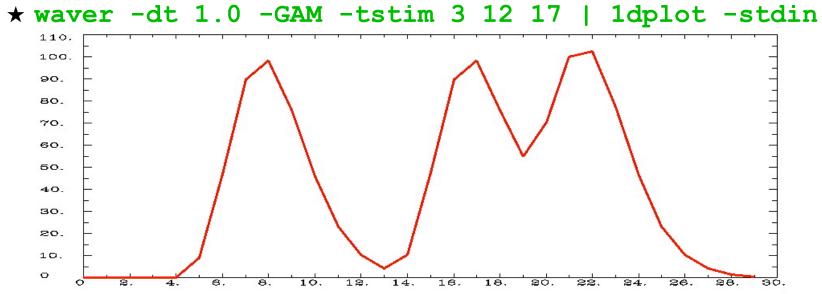
Statistics from 3dDeconvolve

- An F-statistic measures significance of how much a model component reduced the variance of the time series data
- Full F measures how much the signal regressors reduced the variance over just the baseline regressors (sub-brick #0 below)
- Individual partial-model Fs measures how much each individual signal regressor reduced data variance over the full model with that regressor excluded (sub-bricks #19, #22, #25, and #28 below)
- The Coef sub-bricks are the β weights (e.g., #17, #20, #23, #26)
- A t-statistic sub-brick measure impact of one coefficient

```
0 Full F-stat #13 Run #4 t^0 Coe #26 LowC[0] Coef
# 1 Run #1 t^0 Coe #14 Run #4 t^0 t-s #27 LowC[0] t-st
 2 Run #1 t^0 t-s #15 Run #4 t^1 Coe #28 LowC F-stat
 3 Run #1 t^1 Coe #16 Run #4 t^1 t-s #29 AvsT LC[0] coe
 4 Run #1 t^1 t-s #17 Actions[0] Coe #30 AvsT LC[0] t-s
 5 Run #2 t^0 Coe #18 Actions[0] t-s #31 AvsT F-stat
# 6 Run #2 t^0 t-s #19 Actions F-stat #32 HvsL LC[0] coe
# 7 Run #2 t^1 Coe #20 Tool[0] Coef
                                     #33 HvsL LC[0] t-s
# 8 Run #2 t^1 t-s #21 Tool[0] t-st
                                     #34 HvsL F-stat
# 9 Run #3 t^0 Coe #22 Tool F-stat
                                     #35 ATvsHL LC[0] c
#10 Run #3 t^0 t-s #23 HighC[0] Coef
                                     #36 ATvsHL LC[0] t
#11 Run #3 t^1 Coe #24 HighC[0] t-st
                                     #37 ATvsHL F-stat
#12 Run #3 t^1 t-s #25 HighC F-stat
```

Alternative Way to Run waver

- Instead of giving stimulus timing on the TR-grid as a set of 0s and 1s
- Can give the actual stimulus times (in seconds) using the
 tstim option



- If times are in a file, can use -tstim `cat filename` to place them on the command line after -tstim option
 - ★ This is most useful for event-related experiments

Note backward single quotes

Deconvolution Signal Models

- Simple or Fixed-shape regression:
 - ★ We fixed the shape of the HRF
 - ★ Used waver to generate the signal model from the stimulus timing
 - ★ Found the amplitude of the signal model in each voxel
- Deconvolution or Variable-shape regression:
 - ★ We allow the shape of the HRF to vary in each voxel, for each stimulus class
 - ★ Appropriate when you don't want to overconstrain the solution by assuming an HRF shape
 - ★ Caveat: need to have enough time points during the HRF in order to resolve its shape

Deconvolution: Pros and Cons

- + Letting HRF shape varies allows for subject and regional variability in hemodynamics
- + Can test HRF estimate for different shapes; e.g., are later time points more "active" than earlier?
- Need to estimate more parameters for each stimulus class than a fixed-shape model (e.g., 4-15 vs. 1 parameter=amplitude of HRF)
- Which means you need more data to get the same statistical power (assuming that the fixedshape model you would otherwise use was in fact "correct")
- Freedom to get any shape in HRF results can give weird shapes that are difficult to interpret

Expressing HRF via Regression Unknowns

 The tool for expressing an unknown function as a finite set of numbers that can be fit via linear regression is an <u>expansion in basis functions</u>

$$h(t) = \beta_0 \psi_0(t) + \beta_1 \psi_1(t) + \beta_2 \psi_2(t) + \dots = \sum_{q=0}^{q-p} \beta_q \psi_q(t)$$

- \star The basis functions $\psi_q(t)$ are known, as is the expansion order p
- * The unknowns to be found (in each voxel) comprises the set of weights β_q for each $\psi_q(t)$
- Since β weights appear only by multiplying known values, and HRF only appears in final signal model by linear convolution, resulting signal model is still solvable by linear regression

Basis Function: "Sticks"

- The set of basis functions you use determines the range of possible HRFs that you can compute
- "Stick" (or Dirac delta) functions are very flexible
 - But they come with a strict limitation
- $\delta(t)$ is 1 at t=0 and is 0 at all other values of t

 $\rightarrow h(t) = 0$ for any t not on the TR grid

Sticks: Good Points

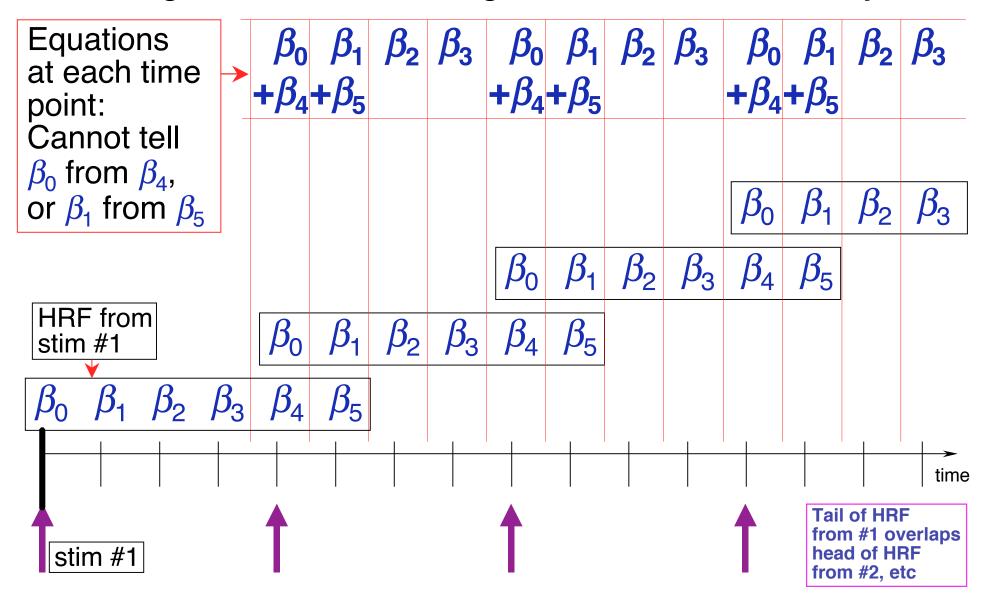
- Can represent arbitrary shapes of the HRF, up and down, with ease
- Meaning of each β_a is completely obvious
 - ★ Value of HRF at time lag q·TR after activation
- 3dDeconvolve is set up to deal with stick functions for representing HRF, so using them is very easy
 - What is called p here is given by command line option -stim_maxlag in the program
 - When choosing *p*, rule is to estimate longest duration of neural activation after stimulus onset, then add 10-12 seconds to allow for slowness of hemodynamic response

Sticks and TR-locked Stimuli

- h(t) = 0 for any t not on the TR grid
- This limitation means that, using stick functions as our basis set, we can only model stimuli that are "locked" to the TR grid
 - ★ That is, stimuli/activations don't occur at fully general times, but only occur at integer multiples of TR
- For example, suppose an activation is at t=1.7-TR
 - * We need to model the response at later times, such as $2 \cdot TR$, $3 \cdot TR$, etc., so need to model h(t) at times such as $t=(2-1.7) \cdot TR=0.3 \cdot TR$, $t=1.3 \cdot TR$, etc., after the stimulus
 - But the stick function model doesn't allow for such intermediate times
 - or, can allow Δt for sticks to be a fraction of TR for data
 - e.g., $\Delta t = TR/2$, which implies twice as many β_q parameters to cover the same time interval (time interval needed is set by hemodynamics)
 - then would allow stimuli that occur on TR-grid or halfway in-between

Deconvolution and Collinearity

Regular stimulus timing can lead to collinearity!



3dDeconvolve with Stick Functions

- Instead of inputting a signal model time series (e.g., created with waver and stimulus timing), you input the stimulus timing directly
 - ★ Format: a text file with 0s and 1s, 0 at TR-grid times with no stimulus, 1 at time with stimulus
- Must specify the maximum lag (in units of TR) that we expect HRF to last after each stimulus
 - ★ This requires you to make a judgment about the activation — brief or long?
- 3dDeconvolve returns estimated values for each β_q for each stimulus class
 - ★ Usually then use a GLT to test the HRF (or pieces of it) for significance

- -stim_maxlag k p = option to set the maximum lag to p
 for stimulus timing file #k for k=0,1,2,...
 - ★ Stimulus timing file input using command line option
 -stim file k filename as before
 - ★ Can also use -stim_minlag k m option to set the minimum lag if you want a value m different from 0
 - ★ In which case there are p-m+1 parameters in this HRF
- -stim_nptr k r = option to specify that there are r
 stimulus subintervals per TR, rather than just 1
 - ★ This feature can be used to get a finer grained HRF, at the cost of adding more parameters that need to be estimated
 - Need to make sure that the input stimulus timing file (from -stim file) has r entries per TR
 - TR for -stim file and for output HRF is data TR ÷ r

Script for Deconvolution - The Data

- cd AFNI_data2
 - ★ data is in ED/ subdirectory (10 runs of 136 images, TR=2 s)
 - ★ script in file @analyze ht05
 - o stimuli timing and GLT contrast files in misc_files/
 - * start script **now** by typing source @analyze_ht05
 - o will discuss details of script while it runs
- This is an event-related study from Mike Beauchamp (LBC/NIMH)
 - ★ Four classes of stimuli (short videos)
 - Tools moving (e.g., a hammer pounding) TM
 - People moving (e.g., jumping jacks) HM
 - Points outlining tools moving (no objects, just points) <u>TP</u>
 - Points outlining people moving <u>HP</u>
 - ★ Goal is to find if there is an area that distinguishes natural motions (HM and HP) from simpler rigid motions (TM and TP)

Script for Deconvolution - Outline

- Registration of each imaging run (there are 10): 3dvolreg
- Smooth each volume in space (136 sub-bricks per run):
 3dmerge
- Create a brain mask: 3dAutomask and 3dcalc
- Rescale each voxel time series in each imaging run so that its average through time is 100: 3dTstat and 3dcalc
 - \star If baseline is 100, then a β_q of 5 (say) indicates a 5% signal change in that voxel at time laq #q after stimulus
- Catenate all imaging runs together into one big dataset (1360 time points): 3dTcat
- Compute HRFs and statistics: 3dDeconvolve
 - ★ Each HRF will have 15 output points (lags from 0 to 14) with a TR of 1.0 s, since the input data has a TR of 2.0 s and we will be using the -stim_nptr k r option with r=2
- Average together central points 4..9 of each separate HRF to get peak % change in each voxel: 3dTstat

```
#!/bin/tcsh
if ( $#argv > 0 ) then
    set subjects = ( $argv )
else
    set subjects = ED
endif
```

This script is designed to run analyses on a lot of subjects at once. We will only analyze the ED data here. The other subjects will be included in the Group Analysis presentation.

First step is to change to the directory that has this subject's data

```
# volume register and time shift our datasets, and remove the first
# two time points
                                           Loop over imaging runs 1..10
foreach run ( `count -digits 1 1 10` )
   3dvolreg -verbose
                                               Image registration
       -base {$subj} r{$run}+orig'[2]'
                                               of each run to its
       -tshift 0
                                               #2 sub-brick
       -prefix {$subj}_r{$run}_vr
       {$subj} r{$run}+orig'[2..137]'
# will store run data in runs orig directory
# smooth data with 3dmerge.
                                                Lightly blur each dataset
   3dmerge -1blur rms 4
                                                to reduce noise and
            -doall
            -prefix {$subj} r{$run} vr bl
                                                increase functional
            {$subj}_r{$run}_vr+orig
                                                overlap between runs
end
                                                and subjects
    End of loop over imaging runs
```

```
# create masks for each run using 3dAutomask
                                          Loop over imaging runs 1..10
foreach run ( `count -digits 1 1 10`
    3dAutomask -prefix mask r{$run} {$subj} r{$run} vr bl+orig
end
# create a mask enveloping masks of the individual runs
3dcalc -a mask r1+orig -b mask r2+orig -c mask r3+orig
       -d mask r4+orig -e mask r5+orig -f mask r6+orig
       -q mask r7+oriq -h mask r8+oriq -i mask r9+oriq
       -j mask r10+orig
       -expr 'step(a+b+c+d+e+f+q+h+i+j)'
       -prefix full mask
                              This mask dataset will be 1 inside
                              the largest contiguous high intensity
                              EPI region, and 0 outside that
                              region — this makes a brain mask
```

```
# re-scale each run's baseline to 100.
# If baseline is 100, and result of 3dcalc on one voxel is 106, then
# we can say that at that voxel shows a 6% increase is signal activity
# relative to baseline.
# Use full mask to remove non-brain
                                                Mean of the run<sup>th</sup> dataset,
                                                through time: run=1..10
foreach run ( `count -digits 1 1 10` )
    3dTstat -prefix mean r{$run} {$subj} r{$run} vr bl+orig

    Divide each voxel

    3dcalc -a {$subj} r{$run} vr bl+orig
                                                  value ('a') by its
            -b mean r{$run}+orig
                                                  temporal mean ('b') and
            -c full mask+orig
            -expr "(a/b * 100) * c"
                                                  scale by 100
            -prefix scaled r{$run}

    Result will have

                                                  temporal mean of 100
    /bin/rm mean r{$run}+orig*

    Voxels not in the mask

end
                                                  will be set to 0 (by 'c')
```

```
Now we can concatenate our 10 normalized runs with 3dTcat.
 3dTcat -prefix {$subj} all runs
                                             "Gluing" the runs
     scaled r1+orig scaled r2+orig
                                             together, since
     scaled r3+orig scaled r4+orig
                                             3dDeconvolve only
     scaled r5+orig scaled r6+orig
                                             operates on one input
     scaled r7+orig scaled r8+orig
                                             dataset at a time
     scaled r9+orig scaled r10+orig
# move unneeded run data into separate directories
                                              Gets this stuff out of
mkdir runs orig runs temp
                                              the way so that we
                                              don't see it when we
mv {$subj} r* vr* scaled* runs temp
                                              run AFNI later
mv {$subj} r* runs orig
```

```
# run deconvolution analysis
3dDeconvolve -input {$subj} all runs+orig -num stimts 4
   -stim file 1 ../misc files/all stims.1D'[0]' -stim label 1 ToolMov \
            -stim minlag 1 0 -stim maxlag 1 14 -stim nptr 1 2
   -stim file 2 ../misc files/all stims.1D'[1]' -stim label 2 HumanMov\
            -stim minlag 2 0 -stim maxlag 2 14 -stim nptr 2 2
   -stim file 3 ../misc files/all stims.1D'[2]' -stim label 3 ToolPnt \
            -stim minlag 3 0 -stim maxlag 3 14 -stim nptr 3 2
   -stim file 4 ../misc files/all stims.1D'[3]' -stim_label 4 HumanPnt\
            -stim minlag 4 0 -stim maxlag 4 14 -stim nptr 4 2
   -glt 4 ../misc files/contrast1.1D -glt label 1 FullF
   -qlt 1 ../misc files/contrast2.1D -qlt label 2 HvsT
   -qlt 1 ../misc files/contrast3.1D -qlt label 3 MvsP
   -glt 1 ../misc files/contrast4.1D -glt label 4 HMvsHP
   -glt 1 ../misc files/contrast5.1D -glt label 5 TMvsTP
   -glt 1 ../misc files/contrast6.1D -glt label 6 HPvsTP
   -qlt 1 ../misc files/contrast7.1D -qlt label 7 HMvsTM
   -iresp 1 TMirf -iresp 2 HMirf -iresp 3 TPirf -iresp 4 HPirf
   -full first -fout -tout -nobout -polort 2
   -concat ../misc files/runs.1D
   -progress 1000
   -bucket {$subj} func
```

- Input dataset is the catenated thing created earlier
- There are 4 time series models
- All stimuli time series are in one file with 4 columns:
- ../misc files/all stims.1D
 - The selectors like '[2]' pick out a particular column
 - Each stimulus and HRF will be sampled at TR/2 = 1.0 s, due to the use of -stim nptr k 2 for each k
 - Lag from 0 to 14 is about right for hemodynamic response to a brief stimulus

```
-glt 4 ../misc_files/contrast1.1D -glt_label 1 FullF
-glt 1 ../misc_files/contrast2.1D -glt_label 2 HvsT
-glt 1 ../misc_files/contrast3.1D -glt_label 3 MvsP
-glt 1 ../misc_files/contrast4.1D -glt_label 4 HMvsHP
-glt 1 ../misc_files/contrast5.1D -glt_label 5 TMvsTP
-glt 1 ../misc_files/contrast6.1D -glt_label 6 HPvsTP
-glt 1 ../misc_files/contrast7.1D -glt_label 7 HMvsTM
```

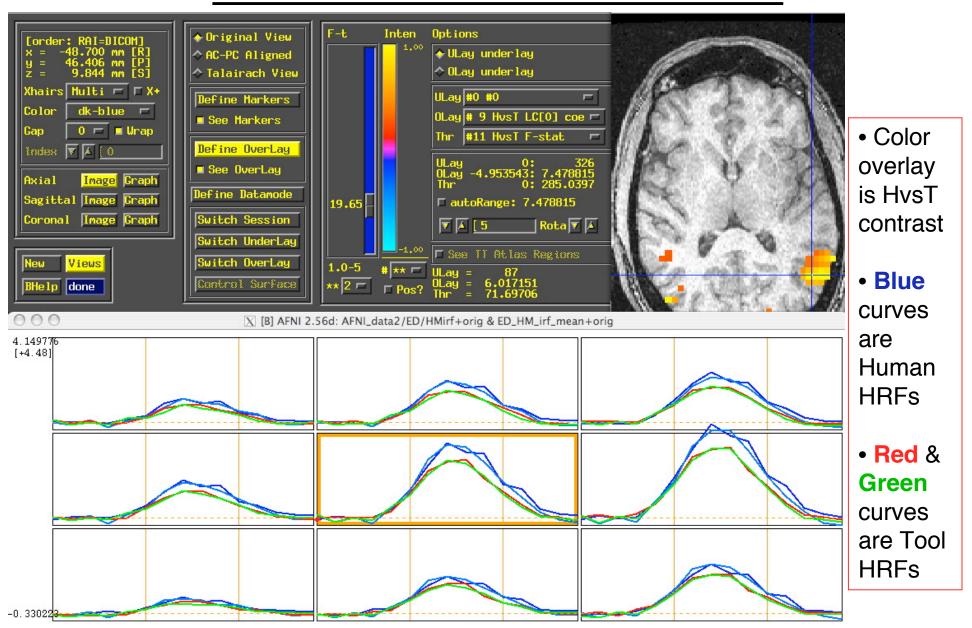
- Run many GLTs to contrast various pairs and quads of cases
 - Each case has 15 points in its HRF, so each GLT needs
 60 inputs indicating how to combine all these β weights
 - Plus 3 zero inputs per imaging run (30 more inputs) to skip over the β weights for the baseline parameters
- One example: HvsT (contrast2.1D) all one line in the file!

```
-iresp 1 TMirf -iresp 2 HMirf -iresp 3 TPirf -iresp 4 HPirf
-full_first -fout -tout -nobout -polort 2
-concat ../misc_files/runs.1D
-progress 1000
-bucket {$subj}_func
```

- Output HRF (-iresp) 3D+time dataset for each stimulus class
 - Each of these datasets will have TR=1.0 s and have 15 time points (lags 0..14)
 - Can plot them atop each other using Dataset#N plugin
- -nobout = don't output statistics of baseline parameters
- -polort 2 = use a quadratic polynomial (3 parameters) for the baseline in each run
- -concat ... = use this file to indicate when each run starts
- -progress 1000 = display some results every 1000th voxel
- -bucket ... = save statistics into dataset with this prefix

```
# make slim dataset. Too many sub-bricks in our bucket dataset.
# Use 3dbucket to slim it down and include sub-bricks of interest only.
3dbucket -prefix {$subj} func slim -fbuc {$subj} func+orig'[125..151]'
# Remember IRF datasets created by 3dDeconvolve?
# There are 15 time lags in each voxel. Remove lags 0-3 and 10-15 b/c not
# interesting. Then find mean percent signal change for lags 4-9 in each
# voxel with '3dTstat'.
# Then transform to Talairach coordinates with 'adwarp'.
  foreach cond (TM HM TP HP)
    3dTstat -prefix {$subj}_{$cond} irf mean {$cond}irf+orig'[4..9]'
    adwarp -apar {$subj}spgr+tlrc -dpar {$subj} {$cond} irf mean+orig
  end
     End of loop over subjects; go back to
end
      upper directory whence we started
# End of script!
# Take the {$subj} {$cond} irf mean+tlrc datasets and input into 3dANOVA2.
```

Results: Humans vs. Tools



More Fun 3dDeconvolve Options

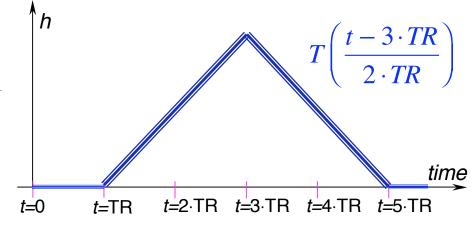
- -mask = used to turn off processing for some voxels
 - * speed up the program by not processing non-brain voxels
- -input1D = used to process a single time series, rather than a dataset full of time series
 - ★ test out a stimulus timing sequence
 - ★ -nodata option can be used to check for collinearity
- -censor = used to turn off processing for some time points
 - ★ for time points that are "bad" (e.g., too much movement)
- -sresp = output standard deviation of HRF estimates
 - * can plot error bands around HRF in AFNI graph viewer
- -errts = output residuals (i.e., difference between fitted model and data)
 - ⋆ for statistical analysis of time series noise
- -jobs N = run with multiple CPUS N of them
 - ★ extra speed, if you have a dual- or quad-processor system!

3dDeconvolve with Free Timing

- The fixed-TR stick function approach doesn't fit with arbitrary timing of stimuli
 - ★ When subject actions/reactions are self-initiated, timing of activations cannot be controlled
- If you want to do deconvolution, then must adopt a different basis function expansion approach
 - \star One that has a finite number of parameters but also allows for calculation of h(t) at any arbitrary point in time
- Simplest set of such functions are closely related to stick

functions: tent functions

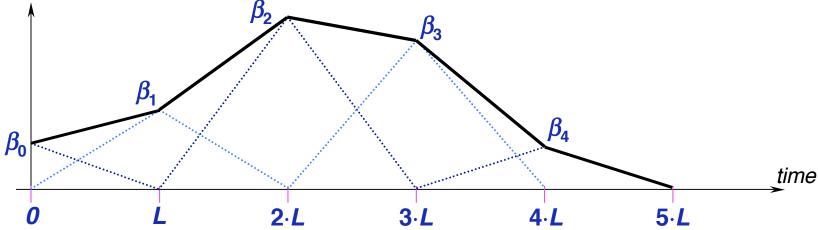
$$T(x) = \begin{cases} 1 - |x| & \text{for } -1 < x < 1 \\ 0 & \text{for } |x| > 1 \end{cases}$$



<u>Tent Functions = Linear Interpolation</u>

 Expansion in a set of spaced-apart tent functions is the same as linear interpolation

$$\beta_0 \cdot T\left(\frac{t}{L}\right) + \beta_1 \cdot T\left(\frac{t-L}{L}\right) + \beta_2 \cdot T\left(\frac{t-2\cdot L}{L}\right) + \beta_3 \cdot T\left(\frac{t-3\cdot L}{L}\right) + \cdots$$



- Tent function parameters are also easily interpreted as function values
- User must decide on relationship of tent function spacing L and time grid TR

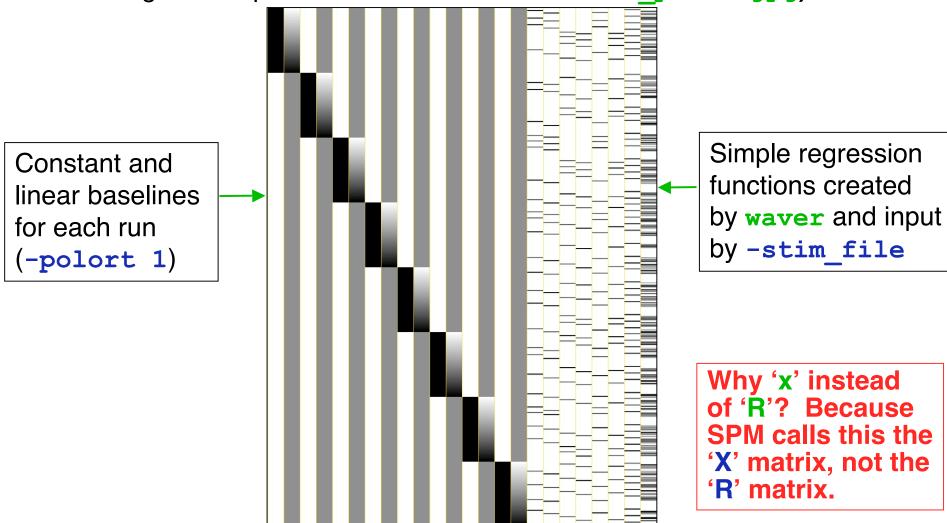
At This Point ...

- 3dDeconvolve is not set up to use tent functions directly
- In the past, we have now explained in grotesque detail
 how to set up a combination of waver, 3dcalc, and
 3dDeconvolve to "trick" the system into doing
 deconvolution with tent functions (or other basis sets)
- However, you are saved from this excruciation
- At this moment, we have an interactive Matlab script that will set up the details for you
- In the near future, we will put tent functions directly into 3dDeconvolve, allowing the direct use of non-TR locked stimulus timing
 - ★ Date of this promise: **13 July 2004** (AFNI Summer Bootcamp)

Upgrades Since July 2004

- See http://afni.nimh.nih.gov/doc/misc/3dDeconvolveSummer2004/
- Equation solver: Gaussian elimination to compute R matrix pseudo-inverse was replaced by SVD (like principal components)
 - ★ Advantage: smaller sensitivity to computational errors
 - ★ "Condition number" and "inverse error" values are printed at program startup, as measures of accuracy of pseudo-inverse
 - ★ Condition number < 1000 is good</p>
 - ★ Inverse error < 1.0e-10 is good
- 3dDeconvolve_f program can be used to compute in single precision (7 decimal places) rather than double precision (16)
 - ★ For better speed, but with lower numerical accuracy
 - ★ Best to do at least one run both ways to check if results differ significantly

 New -xjpeg xxx.jpg option will save a JPEG image file of the columns of the R matrix into file xxx.jpg (and an image of the pseudo-inverse of R into file xxx psinv.jpg)



- Matrix inputs for -glt option can now indicate lots of zero entries using a notation like 30@0 1 -1 0 0 to indicate that 30 zeros precede the rest of the input line
 - ★ Example: 10 imaging runs and -polort 2 for baseline
 - ★ Can put comments into matrix and .1D files, using lines that start with '#' or '//'
 - ★ Can use '\' at end of line to specify continuation
- Matrix input for GLTs can also be expressed symbolically, using the names given with the -stim label options:

```
-stim_label 1 Ear -stim_maxlag 1 4
-stim_label 2 Wax -stim_maxlag 2 4

* Old style GLT might be Sum of Ear - Sum of Wax (lags 2..4)

{zeros for baseline} 0 0 1 1 1 0 0 -1 -1 -1

* New style (via -gltsym option) is
Ear[2..4] -Wax[2..4]
```

- New -xsave option saves the R matrix (and other info) into a file that can be used later with the -xrestore option to calculate some extra GLTs, without re-doing the entire analysis (goal: save some time)
- -input option now allows multiple 3D+time datasets to be specified to automatically catenate individual runs into one file 'on the fly'
 - ★ Avoids having to use program 3dTcat
 - ★ User must still supply full-length .1D files for the various input time series (e.g., -stim file) options
 - ★ -concat option will be ignored if this option is used
 - Break points between runs will be taken as the break points between the various -input datasets
- -polort option now uses Legendre polynomials instead of simple 1, t, t^2 , t^3 , ... basis functions (more numerical accuracy)

- 3dDeconvolve now checks for duplicate -stim_file names and for duplicate matrix columns, and prints warnings
 - ⋆ These are not fatal errors
 - If the same regressor is given twice, each copy will only get half the amplitude (the "beta weight") in the solution
- All zero regressors are now allowed
 - ★ Will get zero weight in the solution
 - A warning message will be printed to the screen
 - ★ Example: task where subject makes a choice for each stimulus
 - You want to analyze correct and incorrect trials a separate cases
 - o What if a subject makes no mistakes?

- Direct input of stimulus timing plus a response model, using new -stim times option
 - ★ -stim_times k tname rtype
 - $\star k = stimulus index (from 1 to -num stimts value)$
 - * tname = name of .1D file containing stimulus times in units of seconds (*important*: TR value in dataset header must be correct!)
 - * rtype = name of response model to use for each stimulus read from tname file
 - GAM = gamma variate function from waver
 - o TENT (b,c,n) = tent function deconvolution, ranging from time s+b to s+c after each stimulus time s, with n basis functions
 - several other rtype options available

- Recall: -iresp option outputs the HRF model for one stimulus
 - ★ When used with -stim_times, values are usually output using the dataset TR time spacing
 - ★ Can changes to a different grid via new -TR_times dt option, which sets the output grid spacing for -iresp to dt for HRF models computed via -stim_times
 - Will be useful for producing nice smooth pictures of HRF
- **<u>Difficulty</u>**: using GLTs with results from -stim_times
 - ★ GLTs operate on regression coefficients
 - ★ For most rtype models, regression coefficients don't correspond directly to HRF amplitudes
 - o Exceptions: GAM, TENT, BLOCK
 - Planned solution: see next slide

<u>Upgrades – Planned or Dreamed of</u>

- Automatic baseline normalization of input time series
- Automatic mask generation (à la 3dAutomask program)
- Spatial blur (à la 3dmerge -1blur)
- Time shift input before analysis (à la 3dTshift program)
- Negative lags for -stim file method of deconvolution
 - ★ for pre-stimulus cognition/anticipation
 - ★ -stim times already allows pre-stimulus response
- 'Area under curve' addition to -gltsym to allow testing of pieces of HRF models from -stim times
- Slice-dependent regressors
 - ★ For physiological noise cancellation
- Floating point output format
 - ★ Currently is shorts + scale factor

Advanced Topics in Regression

 Can have activations with multiple phases that are not always in the same time relationship to each other; e.g.:

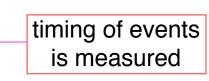
timing of events

is known

- a) subject gets cue #1
- b) variable waiting time ("rest")
- c) subject gets cue #2, emits response
 - → which depends on both cue #1 and #2
- ★ Cannot treat this as one event with one HRF, since the different waiting times will result in different overlaps in separate responses from cue #1 and cue #2
- ★ Solution is multiple HRFs: separate HRF (fixed shape or deconvolution) for cue #1 times and for cue #2 times
 - Must have significant variability in inter-cue waiting times, or will get a nearly-collinear model
 - → impossible to tell tail end of HRF #1 from the start of HRF #2, if always locked together in same temporal relationship
 - How much variability is "significant"? Good question.

More Complicated Case

- Solving a visually presented puzzle:
 - a) subject sees puzzle
 - b) subject cogitates a while
 - c) subject responds with solution



- The problem is that we expect some voxels to be significant in phase (b) as well as phases (a) and/or (c)
- Variable length of phase (b) means that shape for its response varies between trials
 - ★ Which is contrary to the whole idea of averaging trials together to get decent statistics (which is basically what linear regression amounts to)
- Could assume response amplitude in phase (b) is constant across trials, and response duration varies directly with time between phases (a) and (c)
 - ★ Need three HRFs; phase (b)'s is a little tricky to generate using waver, but it could be done

Noise Issues

- "Noise" in FMRI is caused by several factors, not completely characterized
 - ★ MR thermal noise (well understood)
 - ★ Cardiac and respiratory cycles (partly understood)
 - In principle, could measure these sources of noise separately and then try to regress them out
 - → RETROICOR program in progress (Rasmus Birn of FIM)
 - ★ Scanner fluctuations (e.g., thermal drift of hardware)
 - * Small subject head movements (10-100 μm)
 - ★ Very low frequency fluctuations (periods longer than 100 s)
- Data analysis should try to remove what can be removed and allow for the statistical effects of what can't be removed
 - ★ "Serial correlation" in the noise time series affects the t- and F-statistics calculated by 3dDeconvolve
 - ★ At present, nothing is done to correct for this effect (by us)

Nonlinear Regression

- Linear models aren't everything
 - \star e.g., could try to fit HRF of the form $h(t) = a \cdot t^b \cdot e^{-t/c}$
 - ★ Unknowns b and c appear nonlinearly in this formula
- Program 3dNLfim can do nonlinear regression (including nonlinear deconvolution)
 - ★ User must provide a C function that computes the model time series, given a set of parameters (e.g., a, b, c)
 - ★ Program then drives this C function repeatedly, searching for the set of parameters that best fit each voxel
 - ★ Has been used to fit pharmacological wash-in/wash-out models (difference of two exponentials) to FMRI data acquired during pharmacological challenges
 - o e.g., injection of nicotine, cocaine, etc.