

3dDeconvolve

**Advanced Features
Et cetera**

**Just in case you weren't
confused enough already**

Other Features of 3dDeconvolve - 1

- **-input1D** = used to process a single time series, rather than a dataset full of time series
 - ★ e.g., test out a stimulus timing sequence on sample data
 - ★ **-nodata** option can be used to check **X** matrix for collinearity
- ★ **-censor** = used to turn off processing for some time points
 - ★ for time points that are “bad” (e.g., too much movement; scanner problem)
 - ★ **-CENSORTR 2:37** = newer way to specify omissions (e.g., run #2, index #37)
- **-sresp** = output standard deviation of HRF (β) estimates
 - ★ can then plot error bands around HRF in AFNI graph viewer
- **-errts** = output residuals (difference between fitted model and data)
 - ★ for statistical analysis of time series noise
- **-TR_times dt** = calculate **-iresp** and **-sresp** HRF results with time step **dt** (instead of input dataset TR)
 - ★ Can be used to make HRF graphs look better
- ★ **-jobs N** = run with independent threads — **N** of them
 - ★ extra speed, if you have a dual-CPU system (or more)!

Other Features - 2

<http://afni.nimh.nih.gov/pub/dist/doc/misc/Decon/DeconSummer2004.html>

<http://afni.nimh.nih.gov/pub/dist/doc/misc/Decon/DeconSpring2007.html>

- Equation solver: Program computes **condition number** for **X** matrix (measures of how sensitive regression results are to changes in **X**)
 - ★ If the condition number is “bad” (too big), then the program will not actually proceed to compute the results
 - ★ You can use the **-GOFORIT** option on the command line to force the program to run despite **X** matrix warnings
 - But you should strive to understand why you are getting these warnings!!
- Other matrix checks:
 - ★ Duplicate stimulus filenames, duplicate regression matrix columns, all zero matrix columns
- ★ Check the screen output for **WARNINGS** and **ERRORS** ★
 - ★ Such messages also saved into file `3dDeconvolve.err`

Other Features - 3

- ★ All-zero regressors *are* allowed (via `-allzero_OK` or `-GOFORIT`)
 - ★ Will get zero weight in the solution
 - ★ Example: task where subject makes a choice for each stimulus (e.g., male or female face?)
 - You want to analyze correct and incorrect trials as separate cases
 - What if some subject makes no mistakes? Hmmmm...
 - ➔ Can keep the all-zero regressor (e.g., all `-stim_times = *`)
 - ➔ Input files and output datasets for error-making and perfect-performing subjects will be organized the same way

- **3dDeconvolve_f** program can be used to compute linear regression results in single precision (7 decimal places) rather than double precision (16 places)
 - ★ For better speed, but with lower numerical accuracy
 - ★ Best to do at least one run **both** ways to check if results differ significantly (Equation solver *should* be safe, but ...)

Other Features - 4

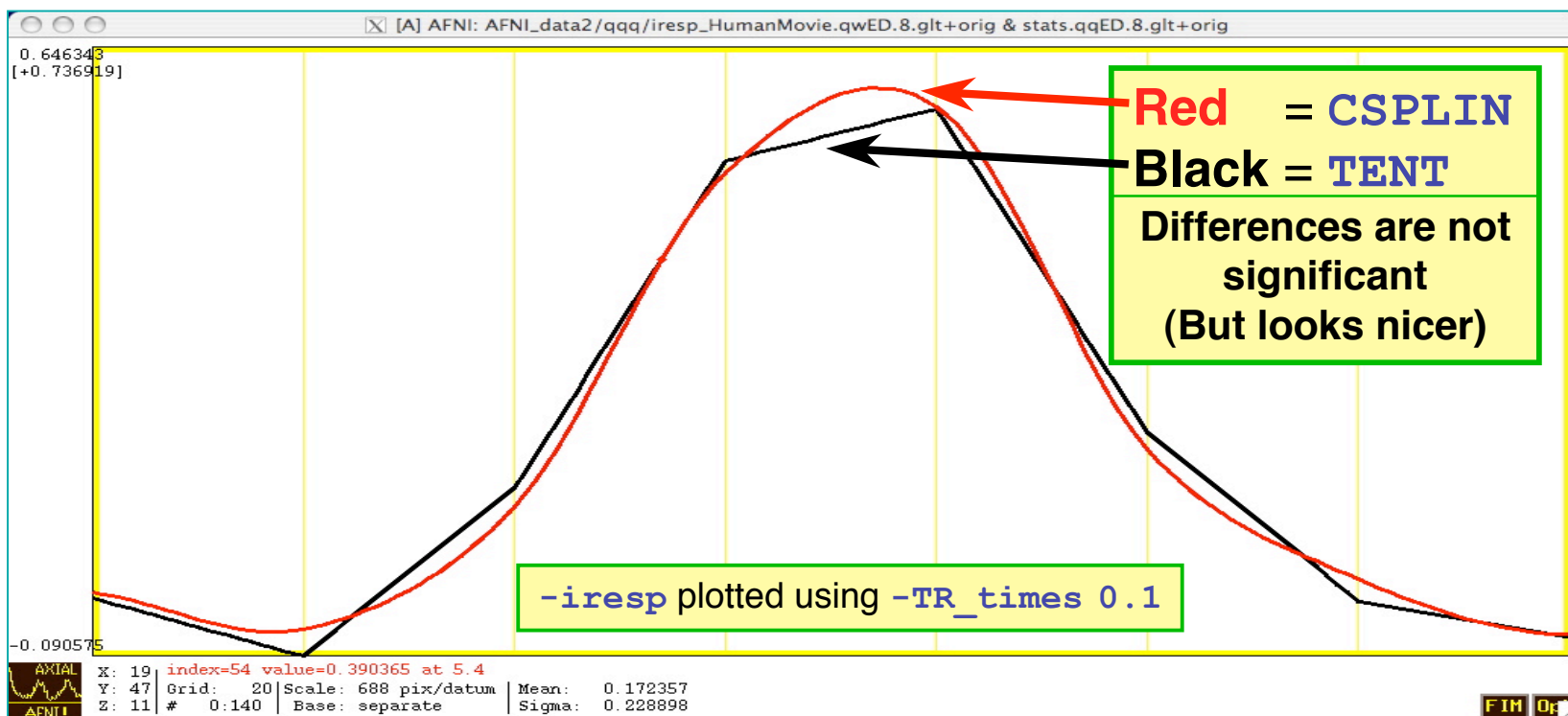
- ★ Default output format is 16-bit short integers, with a scaling factor for each sub-brick to convert it to floating point values
 - ★ `-float` option can be used to get 32-bit floating point format output — more precision, and more disk space

- `3dDeconvolve` recommends a `-polort` value, and prints that out as well as the value you chose (or defaulted to)
 - ★ `-polort A` can be used to let the program set the detrending (AKA “high pass filtering”, since detrending removes low frequency content from data) level automatically

- `-stim_file` is used to input a column directly into **X** matrix
 - ★ Motion parameters (as in previous examples)
 - ★ If you create a stimulus+response model outside `3dDeconvolve` (e.g., using program `waver`)

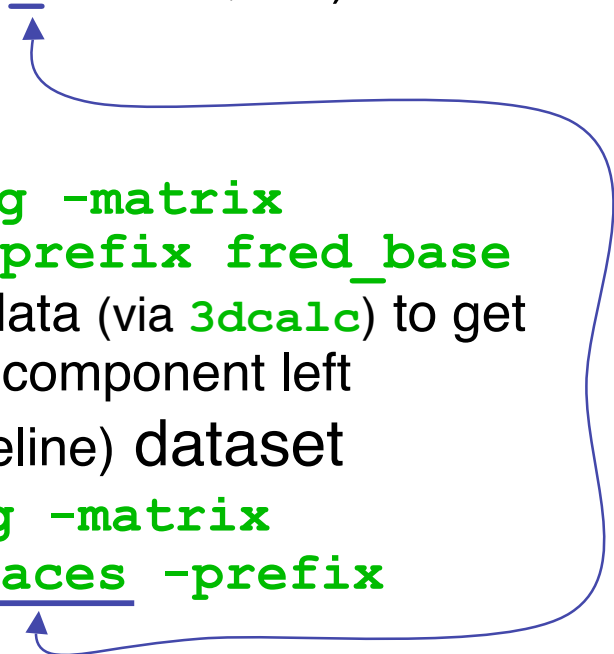
Other Features - 5

- `-stim_times` has some other basis function options for the HRF model besides **BLOCK** and **TENT**
 - ★ **CSPLIN** = cubic spline instead of **TENT** = linear spline
 - Same parameters: (`start, stop, number of regressors`)
 - Can be used as a “drop in” replacement for **TENT**



Other Features - 6

- `-fitts` option is used to create a synthetic dataset
 - ★ each voxel time series is full (signal+baseline) model as fitted to the data time series in the corresponding voxel location

 - `3dSynthesize` program can be used to create synthetic datasets from *subsets* of the full model
 - ★ Uses `-x1D` and `-cbucket` outputs from `3dDeconvolve`
 - `-cbucket` stores β coefficients for each `X` matrix column into dataset
 - `-x1D` stores the matrix columns (and `-stim_labels`, etc.)
 - ★ Potential uses:
 - Baseline only dataset
 - ↳ `3dSynthesize -cbucket fred+orig -matrix fred.xmat.1D -select baseline -prefix fred_base`
 - ↳ Could subtract this dataset from original data (via `3dcalc`) to get signal+noise dataset that has no baseline component left
 - Just one stimulus class model (+ baseline) dataset
 - ↳ `3dSynthesize -cbucket fred+orig -matrix fred.xmat.1D -select baseline Faces -prefix fred_Faces`
- 

Other Recent Small Changes

- Defaults are changed:
 - ★ **-nobout** & **-full_first** & **-bucket** & **-x1D** are always implied
 - ★ Names of statistics sub-bricks are slightly altered (to be more consistent)

- Checks if **-stim_times** inputs are out of range (AKA: the PSFB syndrome)
 - ★ Prints **WARNING** message, but continues analysis

- When using **-nodata** with **-stim_times**, it is important to give the number of time points and the TR, as in **-nodata 250 2.3**
 - ★ With **-input1D**, use **-TR_1D 2.3** to specify TR

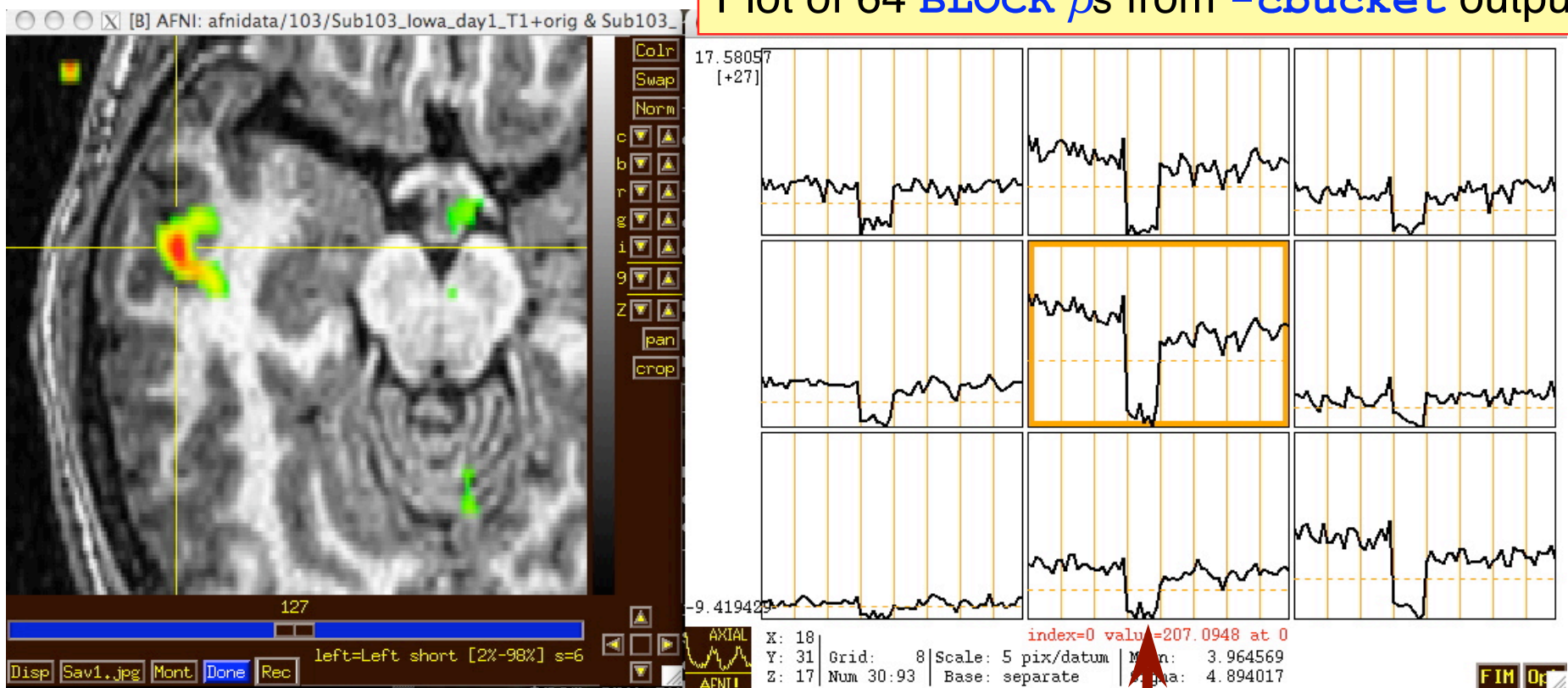
IM Regression - 1

- **IM** = Individual **M**odulation
 - ★ Compute *separate* amplitude of response for each stimulus
 - Instead of computing average amplitude of responses to multiple stimuli in the same class
 - ★ Response amplitudes (β s) for each individual block/event will be highly noisy
 - Can't use individual activation map for much
 - Must pool the computed β s in some further statistical analysis (t -test via **3dttest**? inter-voxel correlations in the β s? correlate β s with something else?)
 - ★ Usage: **-stim_times_IM k tname model**
 - Like **-stim_times**, but creates a separate regression matrix column for each time given

IM Regression - 2

- Only application of IM thus far has been in checking some data we received from another institution
- Experiment: 64 blocks of sensorimotor task (8 runs each with 8 blocks)

Plot of 64 **BLOCK** β s from **-cbucket** output



N.B.: sign reversal in run #4 = stimulus timing error!

IM Regression - 3

- IM works naturally with blocks, which only have 1 amplitude parameter per stimulus
- With event-related experiment and *deconvolution*, have multiple amplitude parameters per stimulus
 - ★ Difficulty: each event in same class won't get the same shaped HRF this way
 - ★ Desideratum: allow response shape to vary (that's deconvolution), but only allow amplitude to vary between responses in the same stimulus class
 - ★ Problem: get unknowns that multiply each other (shape parameters \times amplitude parameters) — and we step outside the realm of *linear* analysis
 - ★ Possible solution: **semi-linear** regression (nonlinear in global shape parameters, linear in local amplitude params)

AM Regression - 1

- **AM** = **A**mplitude **M**odulated (or **M**odulation)
 - ★ Have some extra data measured about each response to a stimulus, and *maybe* the BOLD response amplitude is modulated by this
 - ★ Reaction time; Galvanic skin response; Pain level perception; Emotional valence (happy or sad or angry face?)
 - Want to see if some brain activations vary proportionally to this **ABI** (**A**uxiliary **B**ehaviorial **I**nformation)
-
- Discrete levels (2 or maybe 3) of ABI:
 - ★ Separate the stimuli into sub-classes that are determined by the ABI (“on” and “off”, maybe?)
 - ★ Use a GLT to test if there is a difference between the fMRI responses in the sub-classes

```
3dDeconvolve ... \
  -stim_times 1 regressor_on.1D 'BLOCK(2,1)' -stim_label 1 'On' \
  -stim_times 2 regressor_off.1D 'BLOCK(2,1)' -stim_label 2 'Off' \
  -gltsym 'SYM: +On | +Off' -glt_label 1 'On+Off' \
  -gltsym 'SYM: +On -Off' -glt_label 2 'On-Off' ...
```

- “**On+Off**” tests for any activation in *either* the “on” or “off” conditions
- “**On-Off**” tests for differences in activation *between* “on” and “off” conditions
- Can use **3dcalc** to threshold on **both** statistics at once to find a **conjunction**

AM Regression - 2

- Continuous (or several finely graded) ABI levels
 - ★ Want to find active voxels whose activation level also depends on ABI
 - ★ **3dDeconvolve** is a linear program, so must make the assumption that the change in fMRI signal as ABI changes is linearly proportional to the changes in the ABI values
- Need to make 2 separate regressors
 - ★ One to find the mean fMRI response (the usual `-stim_times` analysis)
 - ★ One to find the variations in the fMRI response as the ABI data varies
- The second regressor should have the form

$$r_{AM2}(t) = \sum_{k=1}^K h(t - \tau_k) \cdot (a_k - \bar{a})$$

- ★ Where a_k = value of k^{th} ABI value, and \bar{a} is the average ABI value
- Response (β) for first regressor is standard activation map
- Statistics and β for second regressor make activation map of places whose BOLD response changes with changes in ABI
 - ★ Using 2 regressors allows separation of voxels that are active but are *not* detectably modulated by the ABI from voxels that *are* ABI-sensitive

AM Regression - 3

- New feature of **3dDeconvolve**: `-stim_times_AM2`
- Use is very similar to standard `-stim_times`
 - ★ `-stim_times_AM2 1 times_ABI.1D 'BLOCK(2,1)'`
 - ★ The `times_ABI.1D` file has time entries that are “married” to ABI values:

10*5	23*4	27*2	39*5
17*2	32*5		
*			
16*2	24*3	37*5	41*4
 - ★ Such files can be created from 2 standard ASCII .1D files using the new **1dMarry** program
 - The `-divorce` option can be used to split them up
- **3dDeconvolve** automatically creates the two regressors (unmodulated and amplitude modulated)
 - ★ Use `-fout` option to get statistics for activation of the pair of regressors (i.e., testing null hypothesis that *both* β weights are zero: that there is no ABI-independent *or* ABI-proportional signal change)
 - ★ Use `-tout` option to test each β weight separately
 - ★ Can **1dplot X** matrix columns to see each regressor

AM Regression - 4

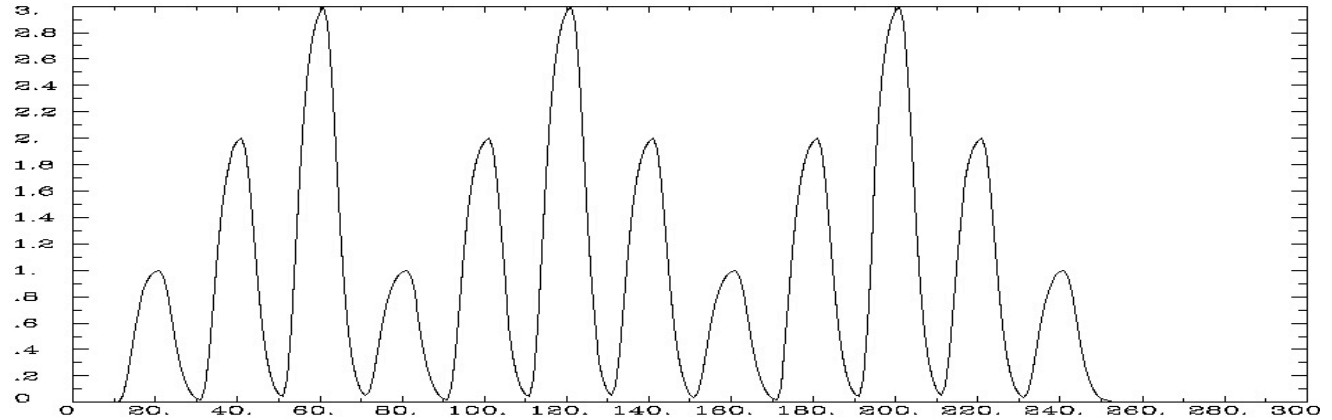
- The **AM** feature is new, and so needs more practical user experiences before it can be considered “standard practice”
 - ★ In particular: don’t know how much data or how many events are needed to get good ABI-dependent statistics
- If you want, `-stim_times_AM1` is also available
 - ★ It only builds the regressor proportional to ABI data directly, with no mean removed:
$$r_{AM1}(t) = \sum_{k=1}^K h(t - \tau_k) \cdot a_k$$
 - ★ Can’t imagine what value this option has, but you never know ... (if you can think of a good use, let me know)
- Future directions:
 - ★ Allow more than one amplitude to be married to each stimulus time (insert obligatory polygamy/polyandry joke here) – **this is done now**
 - How many ABI types at once is too many? I don’t know.
 - ★ How to deal with unknown nonlinearities in the BOLD response to ABI values? I don’t know. (Regress each event separately, then compute MI?)
 - ★ Deconvolution with amplitude modulation? Requires more thought.

AM Regression - 5

Timing: AM.1D = 10*1 30*2 50*3 70*1 90*2 110*3 130*2 150*1 170*2 190*3 210*2 230*1

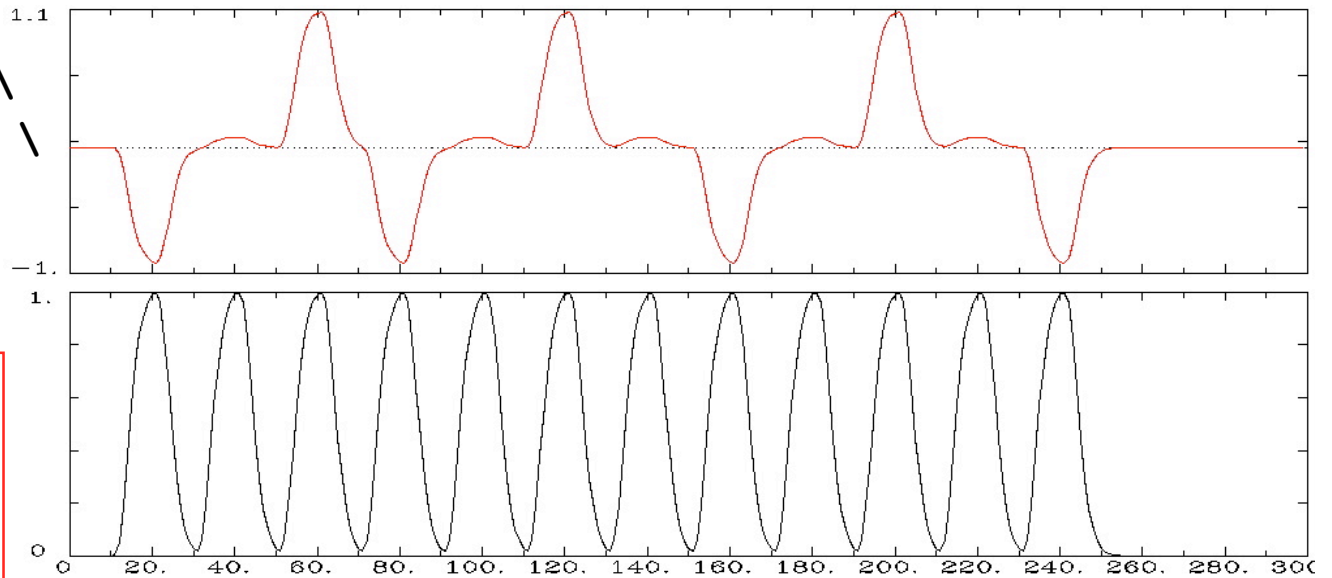
- `3dDeconvolve -nodata 300 1.0 -num_stimts 1 \`
`-stim_times_AM1 1 AM.1D 'BLOCK(10,1)' -x1D AM1.x1D`
- `1dplot AM1.x1D' [2]'`

AM1 model of signal
(modulation = ABI)



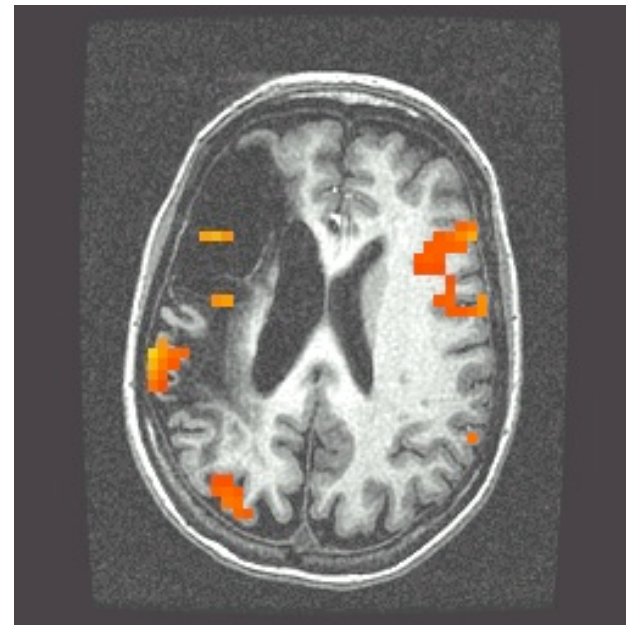
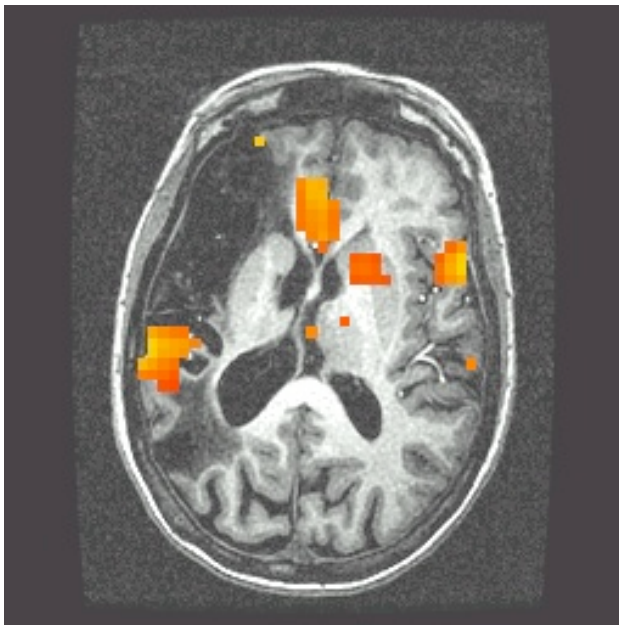
- `3dDeconvolve -nodata 300 1.0 \`
`-num_stimts 1 \`
`-stim_times_AM2 1 \`
`AM.1D 'BLOCK(10,1)' \`
`-x1D AM2.x1D`
- `1dplot -sepscl \`
`AM2.x1D' [2,3]'`

AM2 model of signal:
is 2D sub-space
spanned by these 2
time series



AM Regression - 6

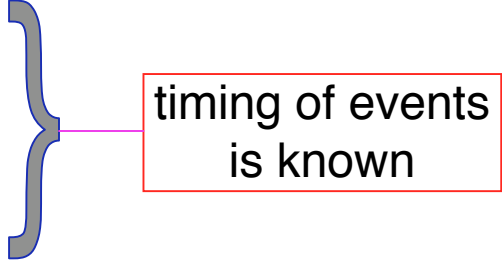
- First actual user: Whitney Postman (formerly NIDCD; PI=Al Braun)
- Picture naming task in aphasic stroke patient
- ABI data = number of alternative names for each image (e.g., “balcony” & “porch” & “veranda”, vs. “strawberry”), from 1 to 18
 - 8 imaging runs, 144 stimulus events
- 2 slices showing activation map for BOLD responses proportional to ABI (β_{AM2})
 - What does this mean? Don't ask me!



AM Regression - 7

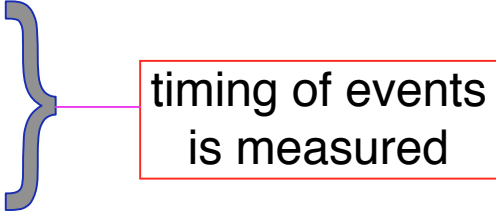
- Alternative: use **IM** to get individual β s for each block/event and then do external regression statistics on those values
- Could do nonlinear fitting (to these β s) via **3dNLfim**, or inter-class contrasts via **3dtttest**, **3dLME**, **3dANOVA**, or intra-class correlations via **3dICC**, etc.
- What is better: **AM** or **IM**+*something more* ?
 - We don't know – experience with these options is limited thus far – you can always try both!
 - If **AM** doesn't fit your models/ideas, then **IM**+ is clearly the way to go
 - Probably need to consult with SSCC to get some hints/advice

Other Advanced Topics in Regression

- Can have activations with multiple phases that are not always in the same time relationship to each other; e.g.:
 - a) subject gets cue #1
 - b) variable waiting time (“hold”)
 - c) subject gets cue #2, emits response
 - ↳ which depends on both cue #1 and #2

timing of events is known
- ★ Cannot treat this as one event with one HRF, since the different waiting times will result in different overlaps in separate responses from cue #1 and cue #2
- ★ Solution is multiple HRFs: separate HRF (fixed shape or deconvolution) for cue #1 times and for cue #2 times
 - Must have significant variability in inter-cue waiting times, or will get a nearly-collinear model
 - ↳ impossible to tell tail end of HRF #1 from the start of HRF #2, if always locked together in same temporal relationship
 - How much variability is “significant”? Good question.

Slightly More Complicated Case

- Solving a visually presented puzzle:
 - a) subject sees puzzle
 - b) subject cogitates a while
 - c) subject responds with solution

timing of events is measured
- The problem is that we expect some voxels to be significant in phase (b) as well as phases (a) and/or (c)
- Variable length of phase (b) means that shape for its response varies between trials
 - ★ Which is contrary to the whole idea of averaging trials together to get decent statistics (which is basically what linear regression for the β weights does, in an elaborate sort of way)
- Could assume response **amplitude** in phase (b) is constant across trials, and response **duration** varies directly with time between phases (a) and (c)
 - ★ Need three HRFs
 - ★ Can't generate (b) HRF in **3dDeconvolve**

Yes we can!
-dmBLOCK model

Noise Issues

- “Noise” in FMRI is caused by several factors, not completely characterized
 - ★ MR thermal noise (well understood, unremovable)
 - ★ Cardiac and respiratory cycles (partly understood)
 - In principle, could measure these sources of noise separately and then try to regress them out
 - ↳ RETROICOR program underway (Rasmus Birn of FIM/NIMH)
 - ★ Scanner fluctuations (e.g., thermal drift of hardware)
 - ★ Small subject head movements (10-100 mm)
 - ★ Very low frequency fluctuations (periods longer than 100 s)
- Data analysis should try to remove what can be removed and should allow for the statistical effects of what can't be removed
 - ★ “Serial correlation” in the noise time series affects the t - and F -statistics calculated by **3dDeconvolve**
 - ★ Next slides: new AFNI program for dealing with this issue

Allowing for Serial Correlation

- t - and F -statistics denominators: estimates of noise variance
 - ★ White noise estimate of variance:
 - N = number of time points
 - m = number of fit parameters
 - $N-m$ = degrees of freedom = how many equal-variance independent random values are left after the time series is fit with m regressors
- **Problem:** if noise values at successive time points are correlated, this estimate of variance is biased to be too small, since there aren't really $N-m$ independent random values left
 - ★ Denominator too small implies t - and F -statistics are too large!
 - ★ And number of degrees of freedom is also too large.
 - ★ So significance (p -value) of activations in individuals is overstated.
- **Solution #1:** estimate correlation structure of noise and then adjust statistics (downwards) appropriately
- **Solution #2:** estimate correlation structure of noise **and** also estimate β fit parameters using more efficient “generalized least squares”, using this correlation, all at once (REML method)

$$\hat{\sigma}^2 = \frac{1}{N-m} \sum_{i=0}^{N-1} [\text{data}_i - \text{fit}_i]^2$$

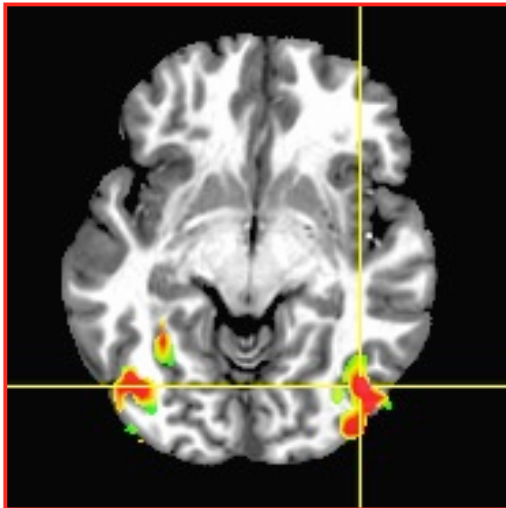
New Program: 3dREMLfit

- Implements Solution #2
 - ★ REML is a method for simultaneously estimating variance + correlation parameters **and** estimating regression fit parameters (β s)
 - ★ Correlation structure of noise is ARMA(1,1)
 - 2 parameters **a** (AR) and **b** (MA) in each voxel
 - ➔ **a** describes how fast the noise de-correlates over time
 - ➔ **b** describes the short-range correlation in time (1 lag)
 - Unlike SPM and FSL, *each voxel* gets a separate estimate of its own correlation parameters
- Inputs to 3dREMLfit
 - ★ run 3dDeconvolve first to setup .xmat.1D matrix file and GLTs (don't have to let 3dDeconvolve finish analysis: `-x1D_stop`)
 - 3dDeconvolve also outputs a command line to run 3dREMLfit
 - ★ then, input matrix file and 3D+time dataset to 3dREMLfit
- Output datasets are similar to those in 3dDeconvolve

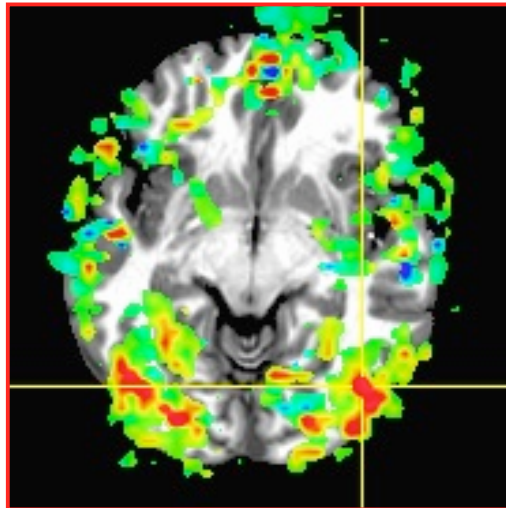
Sample Outputs

- Compare with [AFNI_data3/afni/rall_regress](#) results
- `3dREMLfit -matrix rall_xmat.x1D -input rall_vr+orig -fout -tout \`
`-Rvar rall_varR -Rbuck rall_funcR -Rfitts rall_fittsR \`
`-Obuck rall_funcO -Ofitts rall_fittsO`

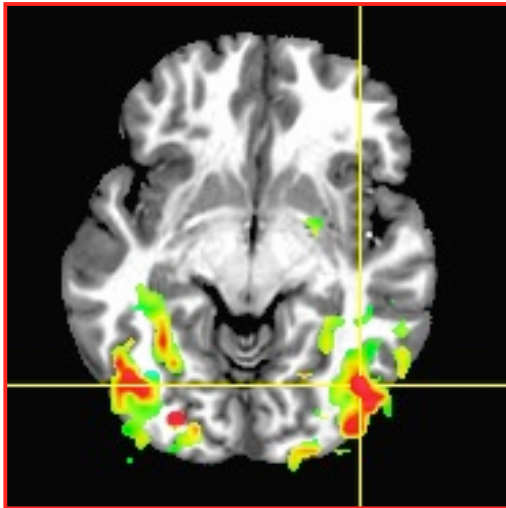
REML
 $F=3.15$
 $p=0.001$



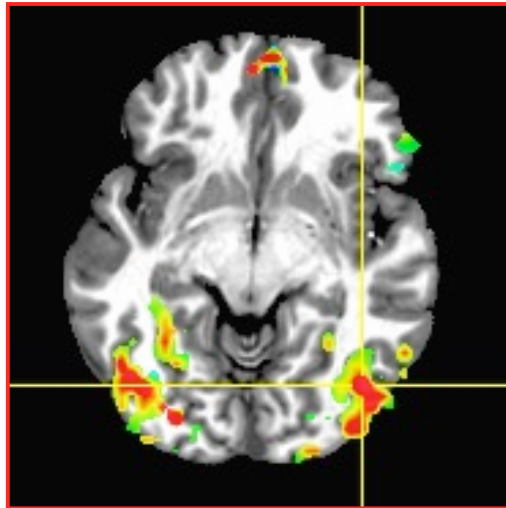
OLSQ
 $F=3.15$
 $p=0.001$



REML
 $F=1.825$
 $p=0.061$
▪ F = No activity outside brain!



OLSQ
 $F=5.358$
 $p=5e-7$
▪ F = No activity outside brain!



**O
h
M
y
G
O
D
!?!**

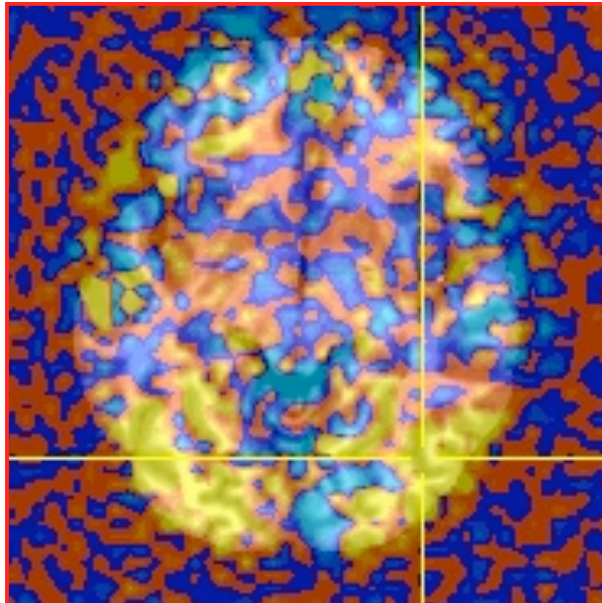
It's Not So Bad: β !

- For individual activation maps, **3dREMLfit**-ized t - and F -statistics are significantly different, and more accurate
- But ... There are at present very few applications for such individual FMRI activation maps
 - ★ pre-surgical planning; some longitudinal study?
- For standard group analysis, inputs are only β fit parameters
 - ★ Which don't change so much between REML and OLSQ

Color Overlay = β weight from analysis on previous slide, no threshold

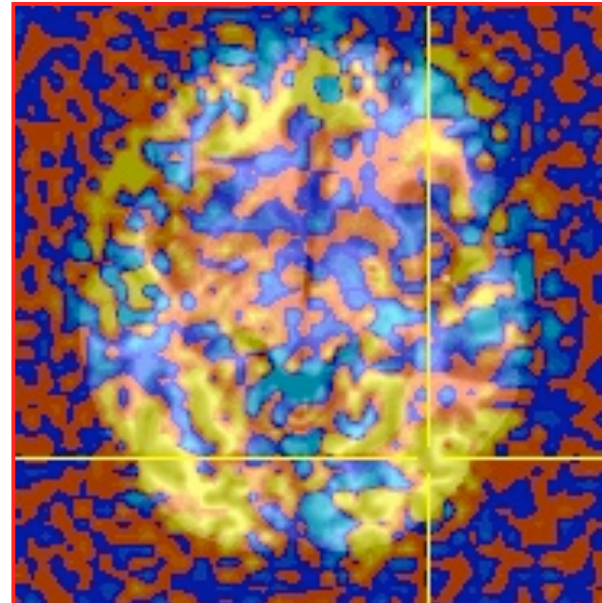
REML

**CPU
500 s**



OLSQ

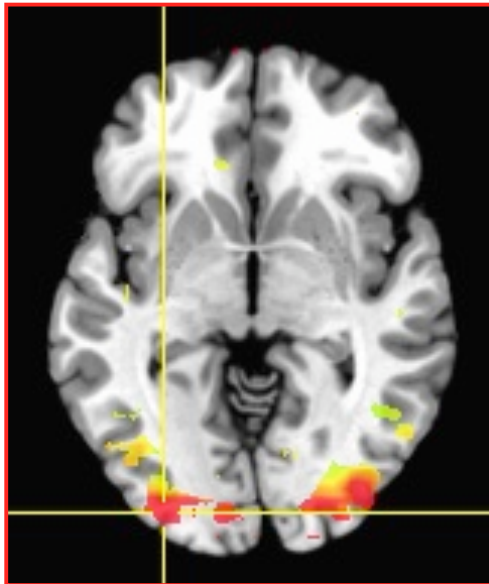
**CPU
156 s**



It's Not So Bad At All: Group Analysis!

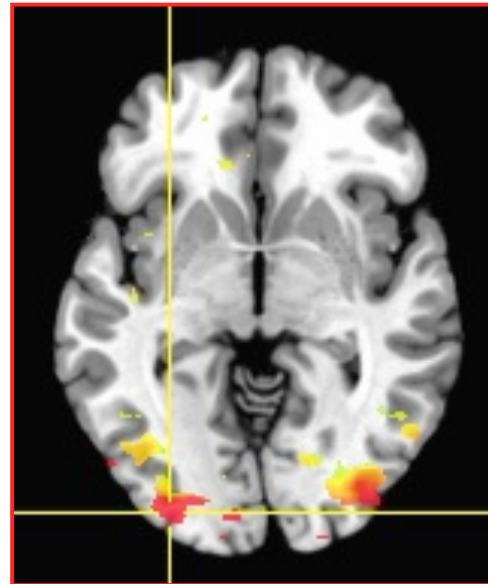
- Group analysis activation maps (**3dANOVA3**) from 16 subjects

REML



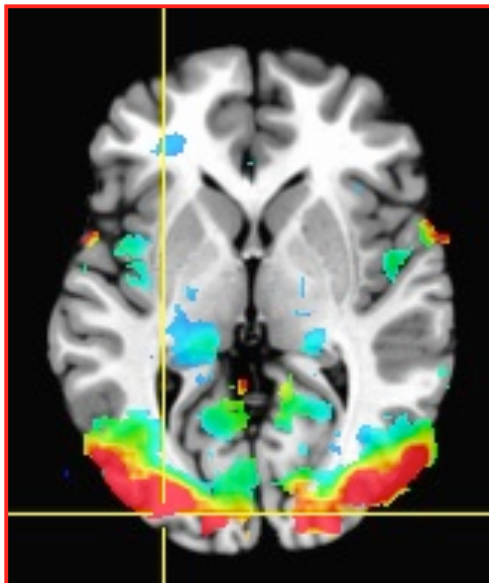
**F-test for
Affect
condition**

OLSQ

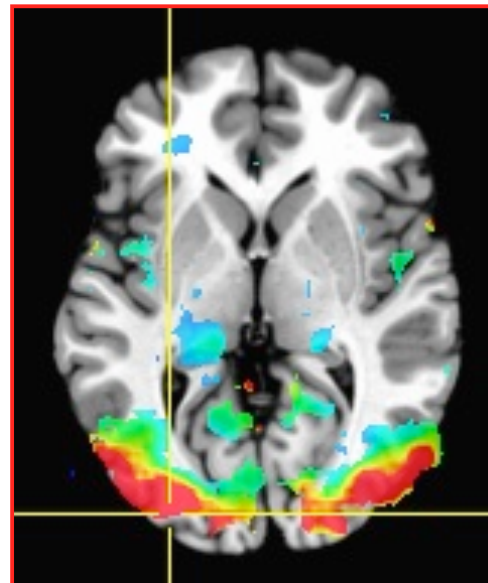


**F-test for
Affect
condition**

**F-test for
Category
condition**



**F-test for
Category
condition**



Nonlinear Regression

- Linear models aren't the only possibility
 - ★ e.g., could try to fit HRF of the form $h(t) = a \cdot t^b \cdot e^{-t/c}$
 - ★ Unknowns b and c appear nonlinearly in this formula
- Program **3dNLFim** can do nonlinear regression (including nonlinear deconvolution)
 - ★ User must provide a C function that computes the model time series, given a set of parameters (e.g., a , b , c)
 - We could help you develop this C model function
 - Several sample model functions in the AFNI source code distribution
 - ★ Program then drives this C function repeatedly, searching for the set of parameters that best fit each voxel
 - ★ Has been used to fit pharmacological wash-in/wash-out models (difference of two exponentials) to fMRI data acquired during pharmacological challenges
 - e.g., injection of nicotine, cocaine, ethanol, etc.
 - these are difficult experiments to do **and** to analyze

Deconvolution: The Other Direction

- Signal model: $Z(t) = H(t)*A(t)$ + baseline model + noise
- $H(t)$ = HRF = response magnitude t seconds after activation
 - ★ $H(t)$ is **causal** = zero for $t < 0$
 - ★ “*” is symbol for convolution, not multiplication!
- **3dDeconvolve**: find out something about $H(t)$ given $A(t)$
- Sometimes (PPI) want to solve the problem in the other direction: assume a model for $H(t)$ and find time series $A(t)$
 - ★ Convolution is commutative: $H(t)*A(t) = A(t)*H(t)$
 - ★ So the other direction looks to be the same problem
 - ★ But isn't, since $H(t)$ is causal but $A(t)$ is not
 - Also, $H(t)*A(t)$ smooths out rough spots in $A(t)$, so undoing this deconvolution adds roughness to the data — including noise, which is already rough — which must be controlled or output $A(t)$ will be junk
- Program **3dTfitter** solves this type of problem
 - ★ Also can allow for *per voxel* baseline model components

Spatial Models of Activation

- Smooth data in space before analysis

- Average data across anatomically-selected regions of interest ROI (before or after analysis)
 - Labor intensive (*i.e.*, hire more students)

- Reject isolated small clusters of above-threshold voxels after analysis

Spatial Smoothing of Data

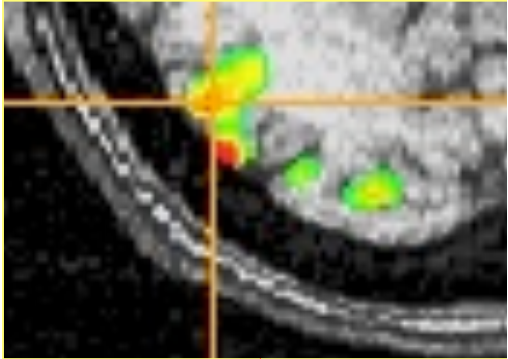
- Reduces number of comparisons

- Reduces noise (by averaging)

- Reduces spatial resolution
 - Blur it enough: Can make fMRI results look like low resolution (1990s) PET data

- Smart smoothing: average **only** over nearby brain or gray matter voxels
 - Uses resolution of fMRI cleverly
 - **3dBlurToFWHM** and **3dBlurInMask**
 - Or: average over selected ROIs
 - Or: cortical surface based smoothing

3dBlurToFWHM

- New program to smooth FMRI time series datasets to a specified smoothness (as estimated by FWHM of noise spatial correlation function)
 - ★ Don't just add smoothness (à la **3dmerge**) but control it (locally and globally)
 - ★ Goal: use datasets from diverse scanners
- Why blur FMRI time series?
 - ★ Averaging neighbors will reduce noise
 - ★ Activations are (usually) blob-ish (several voxels across) 
 - ★ Diminishes the multiple comparisons problem
- **3dBlurToFWHM** and **3dBlurInMask** blur only inside a mask region
 - ★ To avoid mixing air (noise-only) and brain voxels
 - ★ Partial Differential Equation (PDE) based blurring method
 - 2D (intra-slice) or 3D blurring

Spatial Clustering

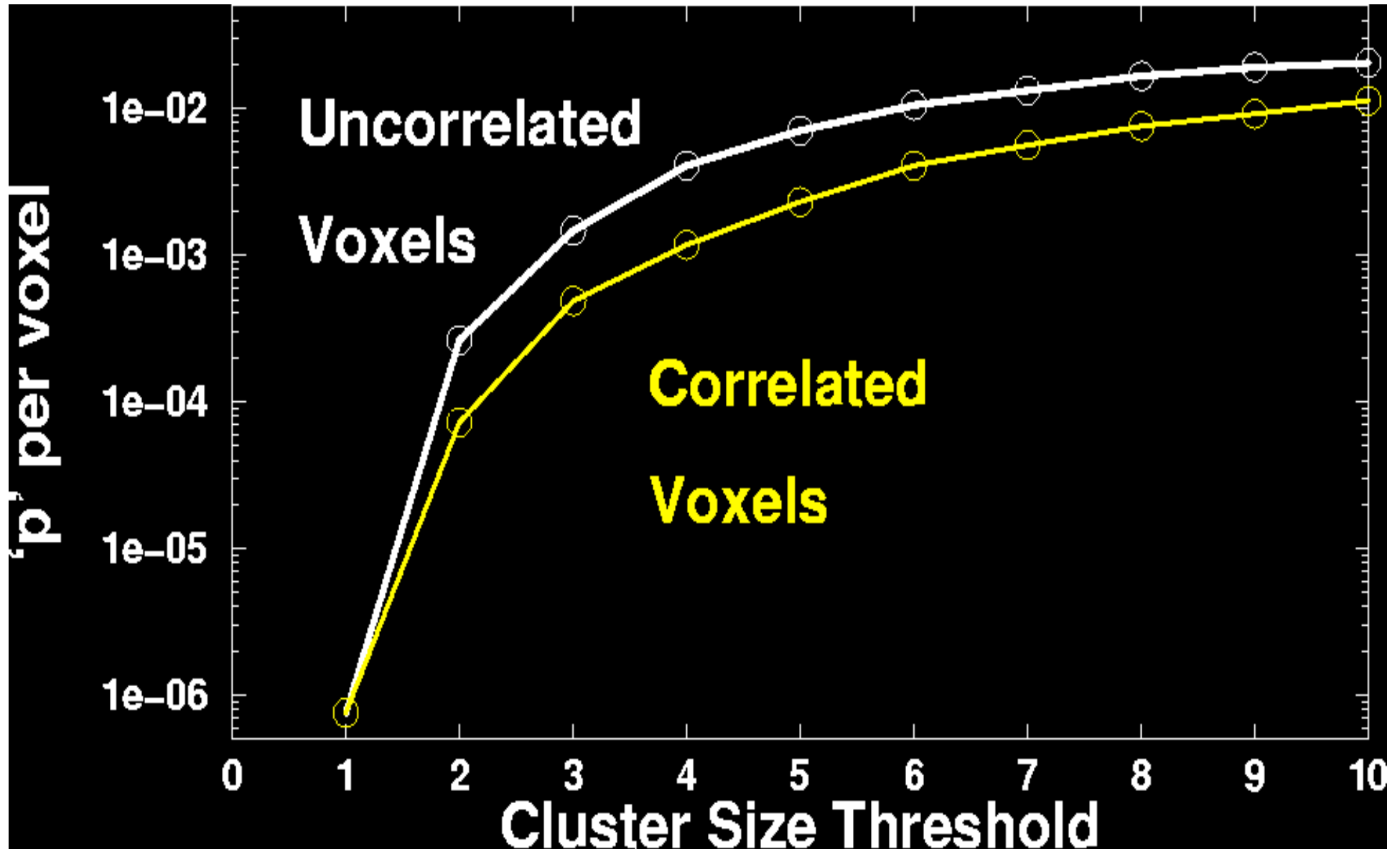
- Analyze data, create statistical map (e.g., t statistic in each voxel)

- Threshold map at a low t value, in each voxel separately
 - Will have many false positives

- Threshold map by rejecting clusters of voxels below a given size

- Can control false-positive rate by adjusting t threshold and cluster-size thresholds together

Cluster-Based Detection






What the World Needs Now

- Unified HRF/Deconvolution ⊕ Blob analysis
 - Time ⊕ Space patterns computed all at once, instead of arbitrary spatial smoothing
 - Increase statistical power by bringing data from multiple voxels together cleverly
 - Instead of time analysis followed by spatial analysis (described earlier)
 - Instead of component-style analyses (e.g., ICA) that do not use stimulus timing

- Difficulty: models for spatial blobs
 - Little information *à priori* ⇒ must be adaptive

In the Thinking Stages

- “Area under curve” addition to `-gltsym` to allow testing of pieces of HRF models from `-stim_times`
- Slice- and/or voxel-dependent regressors
 - ★ For physiological noise cancellation, etc. 
 - ★ To save memory? (Could process each slice separately)
 - One slice-at-a-time regression can be done in a Unix script, using 3dZcutup and 3dZcat programs 
- Extend AM regression to allow for more than 1 piece of auxiliary information at each stimulus time 
- Interactive tool to examine `-x1D` matrix for problems
 - ★ and `3dDeconvolve` testing of GLT submatrices
- Semi-linear deconvolution program

Multi-Voxel Statistics

Spatial Clustering
&

False Discovery Rate:

“Correcting” the Significance

Basic Problem

- Usually have 20-100K FMRI voxels in the brain
- Have to make at least one decision about each one:
 - ★ Is it “active”?
 - That is, does its time series match the temporal pattern of activity we expect?
 - ★ Is it differentially active?
 - That is, is the BOLD signal change in task #1 different from task #2?
- Statistical analysis is designed to control the error rate of these decisions
 - ★ Making *lots* of decisions: hard to get perfection in statistical testing

Multiple Testing Corrections

• **Two types of errors**

- ★ **What is H_0 in FMRI studies?** H_0 : no effect (activation, difference, ...) at a voxel
- ★ Type I error = Prob(reject H_0 when H_0 is true) = false positive = p value
- Type II error = Prob(accept H_0 when H_1 is true) = false negative = β
- power** = $1-\beta$ = probability of detecting true activation
- ★ Strategy: controlling type I error while increasing power (decreasing type II errors)
- ★ Significance level α (magic number 0.05) : $p < \alpha$

Justice System: Trial

Hidden Truth

	Defendant Innocent	Defendant Guilty
Reject Presumption of Innocence (Guilty Verdict)	Type I Error (defendant very unhappy)	Correct
Fail to Reject Presumption of Innocence (Not Guilty Verdict)	Correct	Type II Error (defendant very happy)

Statistics: Hypothesis Test

Hidden Truth

	H_0 True Not Activated	H_0 False Activated
Reject H_0 (decide voxel is activated)	Type I Error (false positive)	Correct
Don't Reject H_0 (decide voxel isn't activated)	Correct	Type II Error (false negative)

- **Family-Wise Error (FWE)**

- ★ Multiple testing problem: voxel-wise statistical analysis

- With N voxels, what is the chance to make a false positive error (Type I) in one or more voxels?

Family-Wise Error: $\alpha_{FW} = 1 - (1 - p)^N \rightarrow 1$ as N increases

- For $N \cdot p$ small (compared to 1), $\alpha_{FW} \approx N \cdot p$
- $N \approx 20,000+$ voxels in the brain
- To keep probability of even one false positive $\alpha_{FW} < 0.05$ (the “corrected” p -value), need to have $p < 0.05 / 2 \times 10^4 = 2.5 \times 10^{-6}$
- This constraint on the per-voxel (“uncorrected”) p -value is so stringent that we’ll end up rejecting a lot of true positives (Type II errors) also, just to be safe on the Type I error rate

- **Multiple testing problem in FMRI**

- ★ 3 occurrences of multiple tests: individual, group, and conjunction
- ★ Group analysis is the most severe situation (have the least data, considered as number of independent samples = subjects)

- **Two Approaches to the “Curse of Multiple Comparisons”**
 - ★ Control **FWE** to keep expected total number of false positives below 1
 - Overall significance: $\alpha_{FW} = \text{Prob}(\geq \text{one false positive voxel in the whole brain})$
 - **Bonferroni correction**: $\alpha_{FW} = 1 - (1-p)^N \approx Np$, if $p \ll N^{-1}$
 - Use $p = \alpha/N$ as individual voxel significance level to achieve $\alpha_{FW} = \alpha$
 - Too stringent and overly conservative: $p = 10^{-8} \dots 10^{-6}$
 - Something to rescue us from this hell of statistical super-conservatism?
 - Correlation: Voxels in the brain are not independent
 - Especially after we smooth them together!
 - Means that Bonferroni correction is *way way* too stringent
 - Contiguity: Structures in the brain activation map
 - We are looking for activated “blobs”: the chance that pure noise (H_0) will give a set of seemingly-activated voxels next to each other is lower than getting false positives that are scattered around far apart
 - Control FWE based on spatial correlation (smoothness of image noise) **and** minimum cluster size we are willing to accept

 - ★ Control false discovery rate (**FDR**)
 - FDR = expected proportion of false positive voxels among all **detected** voxels
 - Give up on the idea of having (almost) no false positives at all

Cluster Analysis: **AlphaSim**

- **FWE control in AFNI**

- ★ Monte Carlo simulations with program **AlphaSim**

- Named for a place where primary attractions are randomization experiments
- Randomly generate some number (*e.g.*, 1000) of brain volumes with white noise (spatially uncorrelated)
 - That is, each “brain” volume is purely in H_0 = no activation
 - Noise images can be blurred to mimic the smoothness of real data
- Count number of voxels that are false positives in each simulated volume
 - Including how many are false positives that are spatially together in clusters of various sizes (1, 2, 3, ...)
- Parameters to program
 - Size of dataset to simulate
 - Mask (*e.g.*, to consider only brain-shaped regions in the 3D brick)
 - Spatial correlation FWHM: from **3dBlurToFWHM** or **3dFWHMx**
 - Connectivity radius: how to identify voxels belonging to a cluster?
 - Default = NN connection = touching faces
 - Individual voxel significance level = uncorrected p -value
- Output
 - Simulated (estimated) **overall significance level** (corrected p -value)
 - Corresponding **minimum cluster size** at the input uncorrected p -value

• **Example:** `AlphaSim -nxyz 64 64 20 -dxyz 3 3 5 \`
`-fwhm 5 -pthr 0.001 -iter 1000 -quiet -fast`

- Output is in 6 columns: focus on 1st and 6th columns (ignore others)
 - ★ 1st column: cluster size in voxels
 - ★ 6th column: alpha (α) = overall significance level = corrected p -value

Cl	Size	Frequency	CumuProp	p/Voxel	Max Freq	Alpha
	1	47064	0.751113	0.00103719	0	1.000000
	2	11161	0.929236	0.00046268	13	1.000000
	3	2909	0.975662	0.00019020	209	0.987000
	4	1054	0.992483	0.00008367	400	0.778000
	5	297	0.997223	0.00003220	220	0.378000
	6	111	0.998995	0.00001407	100	0.158000
	7	32	0.999505	0.00000594	29	0.058000
	8	20	0.999825	0.00000321	19	<u>0.029000</u>
	9	8	0.999952	0.00000126	7	0.010000
	10	2	0.999984	0.00000038	2	0.003000
	11	1	1.000000	0.00000013	1	0.001000

- At this uncorrected $p=0.001$, in this size volume, with noise of this smoothness: the chance of a cluster of size 8 *or larger* occurring by chance alone is 0.029
- May have to run several times with different uncorrected p
 - uncorrected (`-pthr`) $p \uparrow \Leftrightarrow$ required minimum cluster size \uparrow
- See detailed steps at <http://afni.nimh.nih.gov/sscc/gangc/mcc.html>

Interactive Clustering

Report on clusters of above threshold voxels

AFNI: data/verbal/anat+orig & r1_time@1+orig

Clusterize parameters:
 *Clusterize
 Clear Rpt

Cluster Report Table:

#	xyz	Peak	3dclust	Save Table	Clust	Done
1:	189 vox	+10.0 +46.9 +20.6	Jump	Flash	Plot	Save
2:	92 vox	+31.0 -1.9 +20.6	Jump	Flash	Plot	Save
3:	86 vox	+3.0 -13.1 +5.6	Jump	Flash	Plot	Save
4:	49 vox	+3.0 +13.1 -31.9	Jump	Flash	Plot	Save
5:	38 vox	+38.0 +69.4 -58.1	Jump	Flash	Plot	Save
6:	22 vox	+45.0 -35.6 -35.6	Jump	Flash	Plot	Save
7:	20 vox	-46.0 +24.4 +13.1	Jump	Flash	Plot	Save

AFNI: data/verbal/anat+orig

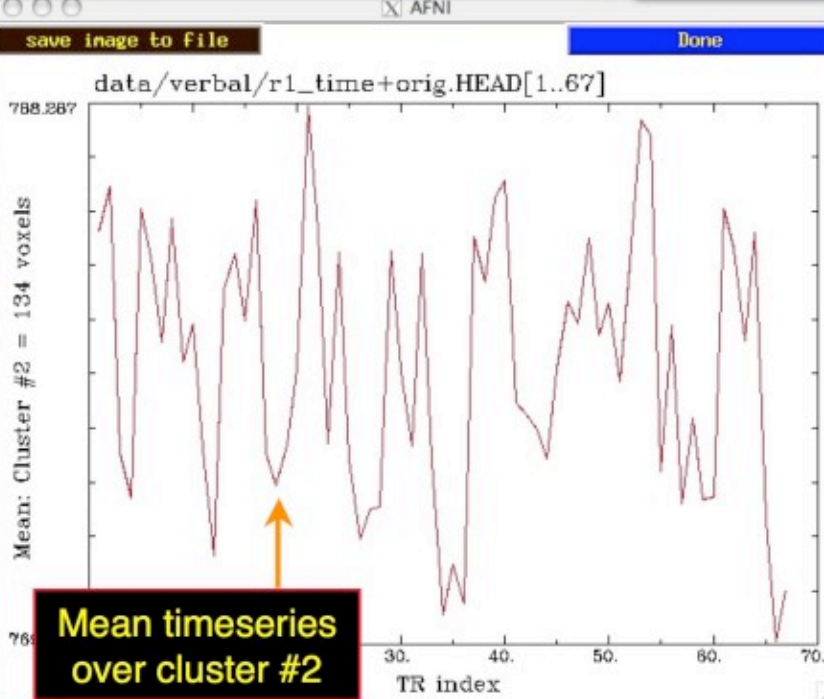
CoIn Swap Norm

Mean: Cluster #2 = 134 voxels

127

Axial: left=Left short [2%-98%]

Disp Savl..Jeg Mont. Done Rec



menu

----- Set Clusterize Parameters -----
 * rnn=0 is Nearest Neighbor clustering; then vnul is cluster volume threshold measured in Overlay voxel count
 * rnn>0 is clustering radius in mm; then vnul = volume threshold in microliters
 * Use 'BHelp' on 'Cluster Edit' label to get summary of clustering results.
 * Click on the 'Rpt' button to open a more complete cluster report panel.

rnn 0
 vnul 20

Quit Apply Set

This panel controls the clustering operation

False Discovery Rate in



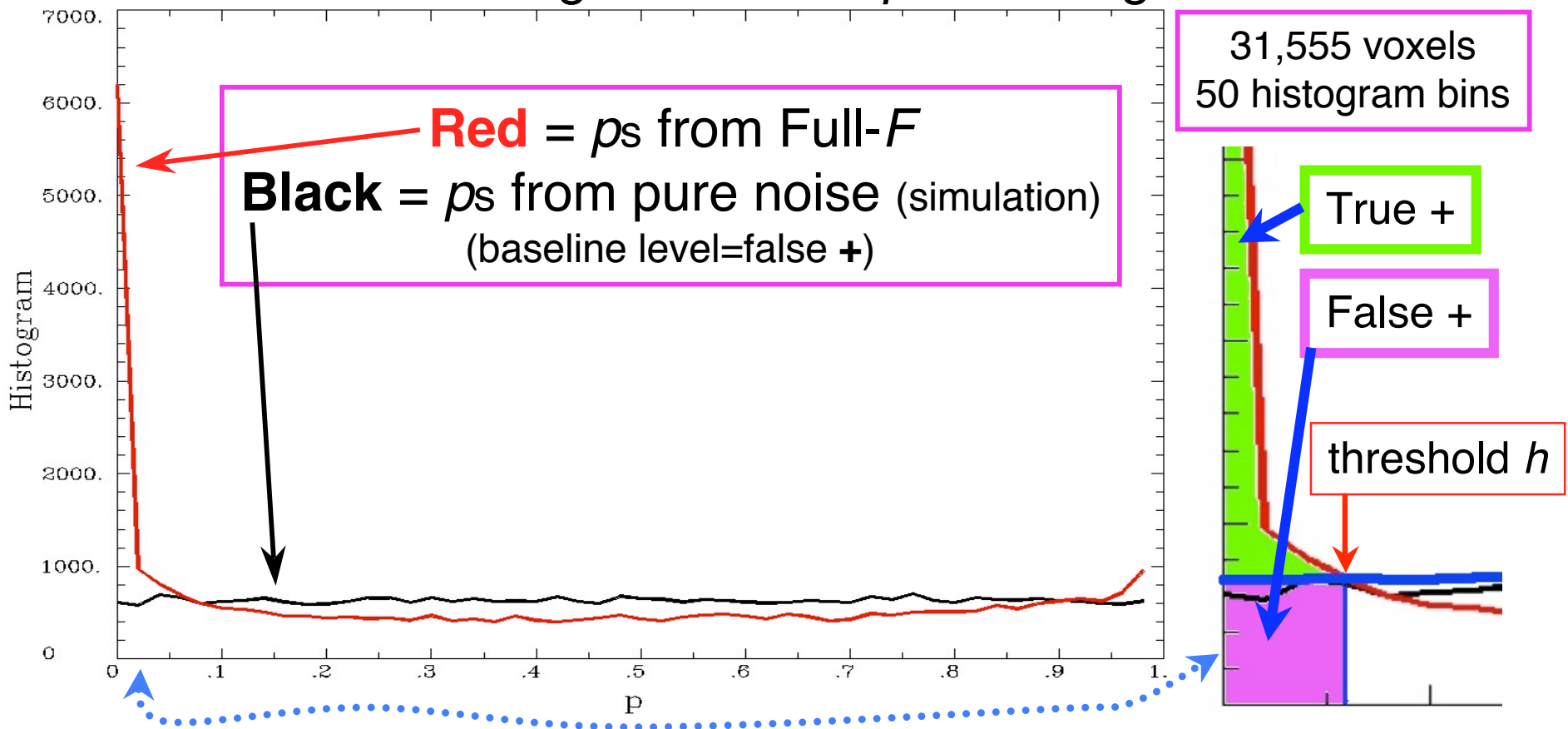
- Situation: making *many* statistical tests at once
 - e.g., Image voxels in FMRI; associating genes with disease
- Want to set threshold on statistic (e.g., *F*- or *t*-value) to control **false positive** error rate
- Traditionally: set threshold to control probability of making a **single** false positive detection
 - But if we are doing 1000s (or more) of tests at once, we have to be very stringent to keep this probability low
- **FDR**: accept the fact that there will be multiple erroneous detections when making lots of decisions
 - Control the **fraction** of positive detections that are wrong
 - Of course, no way to tell which individual detections are right!
 - Or at least: control the *expected value* of this fraction

FDR: q [and $z(q)$]

- Given some collection of statistics (say, F -values from **3dDeconvolve**), set a threshold h
- The **uncorrected p -value** of h is the probability that $F > h$ when the null hypothesis is true (no activation)
 - “Uncorrected” means “per-voxel”
 - The “corrected” p -value is the probability that *any* voxel is above threshold in the case that they are all *unactivated*
 - If have N voxels to test, $p_{\text{corrected}} = 1 - (1 - p)^N \approx Np$ (for small p)
 - o Bonferroni: to keep $p_{\text{corrected}} < 0.05$, need $p < 0.05 / N$, which is very tiny
- The FDR **q -value** of h is the fraction of false positives expected when we set the threshold to h
 - Smaller q is “better” (more stringent = fewer false detections)
 - $z(q)$ = conversion of q to Gaussian z -score: e.g, $z(0.05) \approx 1.95996$
 - o So that larger is “better” (in the same sense): e.g, $z(0.01) \approx 2.57583$

Basic Ideas Behind FDR q

- **If** all the null hypotheses are true, **then** the statistical distribution of the p -values will be uniform
 - Deviations from uniformity at low p -values \Rightarrow true positives
 - Baseline of uniformity indicates how many true negatives are hidden amongst in the low p -value region

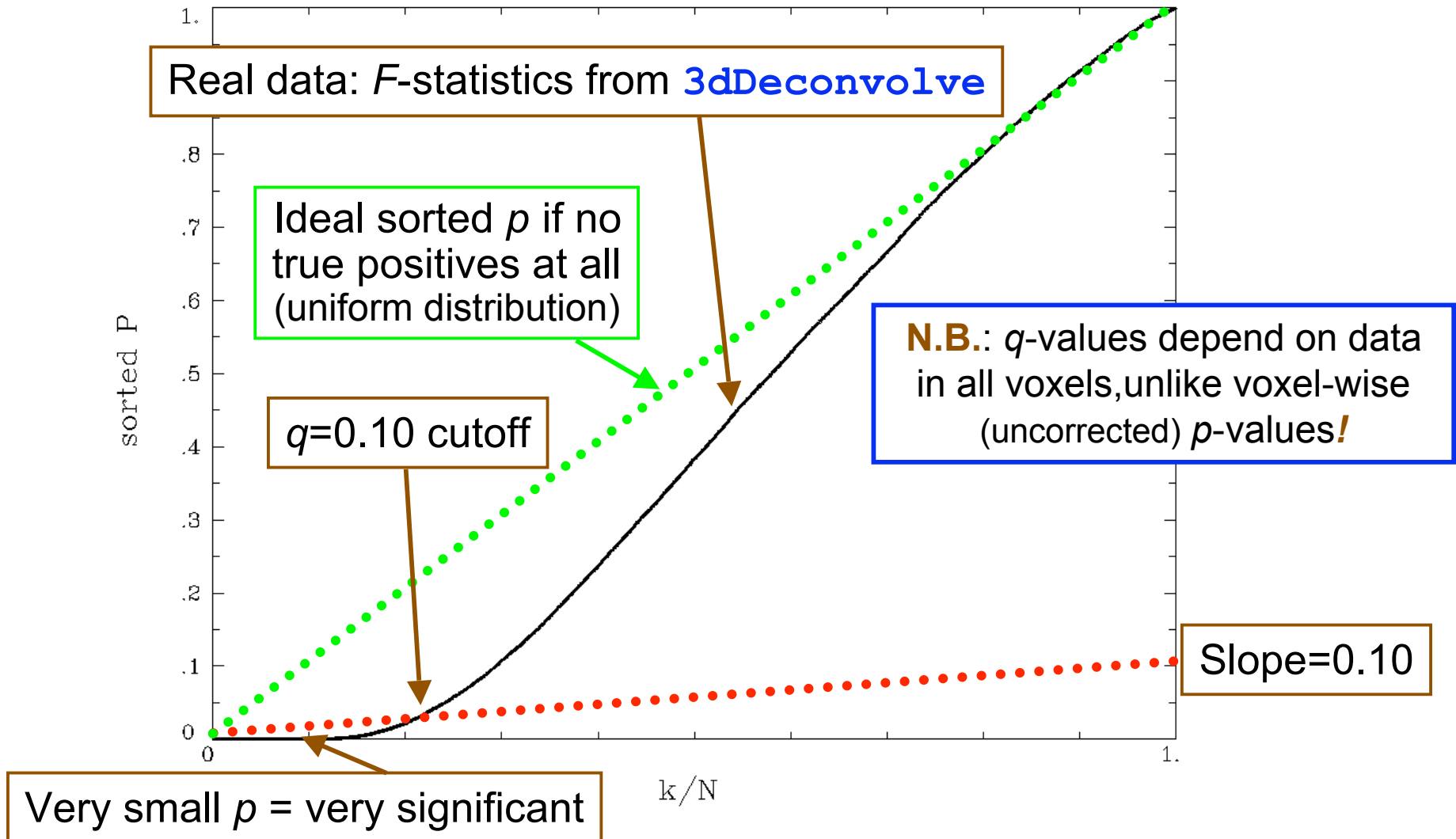


How q is Calculated from Data

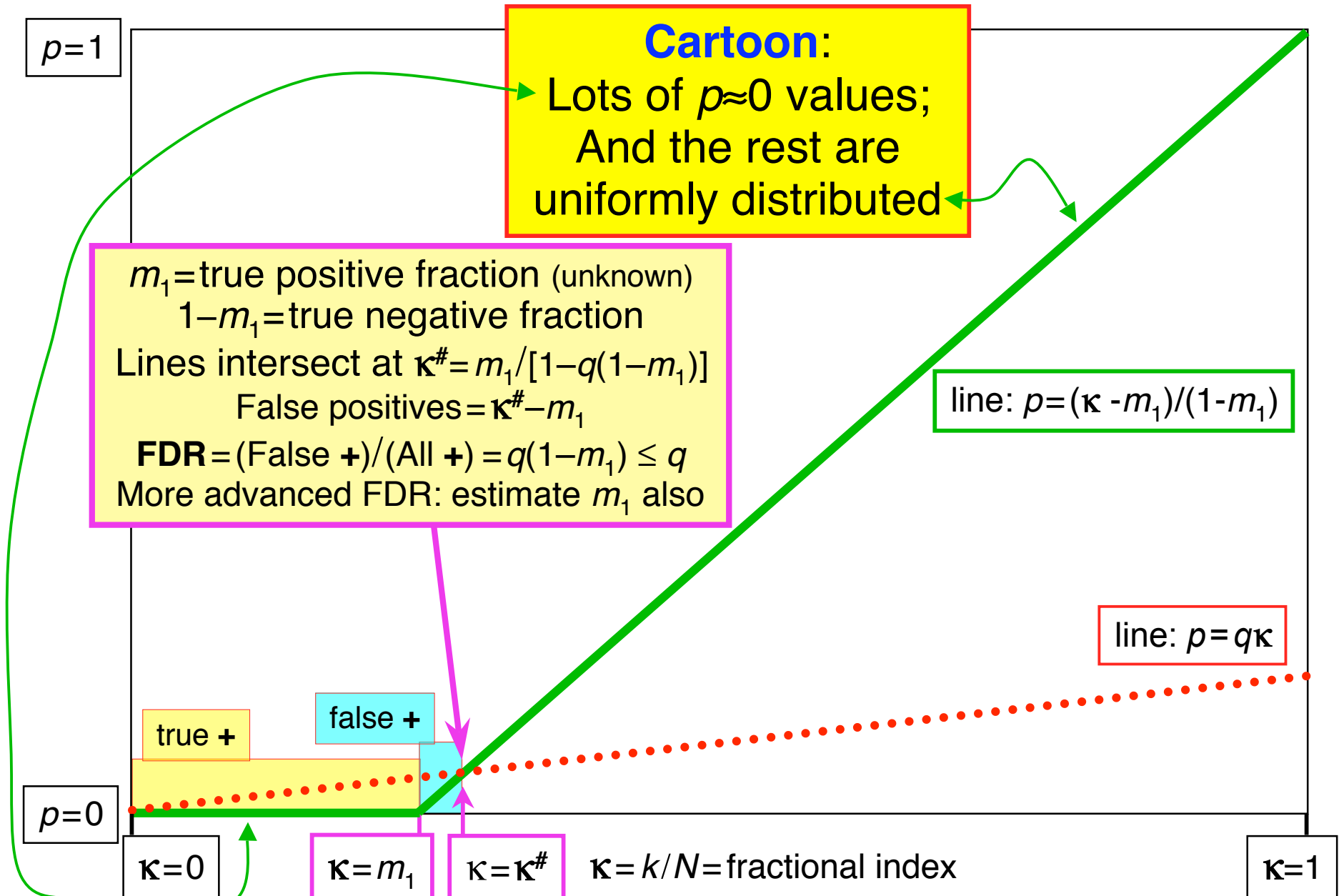
- Compute p -values of each statistic: $P_1, P_2, P_3, \dots, P_N$
- Sort these: $P_{(1)} \leq P_{(2)} \leq P_{(3)} \leq \dots \leq P_{(N)}$ {subscript_() \equiv sorted}
- For $k = 1..N$, $q_{(k)} = \min_{m \geq k} [N \cdot P_{(m)} / m]$
 - Easily computed from sorted p -values by looping downwards from $k = N$ to $k = 1$
- By keeping track of voxel each $P_{(k)}$ came from: can put q -values (or $z(q)$ values) back into image
 - This is exactly how program **3dFDR** works
- By keeping track of statistic value (t or F) each $P_{(k)}$ came from: can create curve of threshold h vs. $z(q)$
- **N.B.:** q -values depend on the data in ***all*** voxels, unlike these voxel-wise (uncorrected) p -values!
 - Which is why it's important to mask brain properly

Graphical Calculation of q

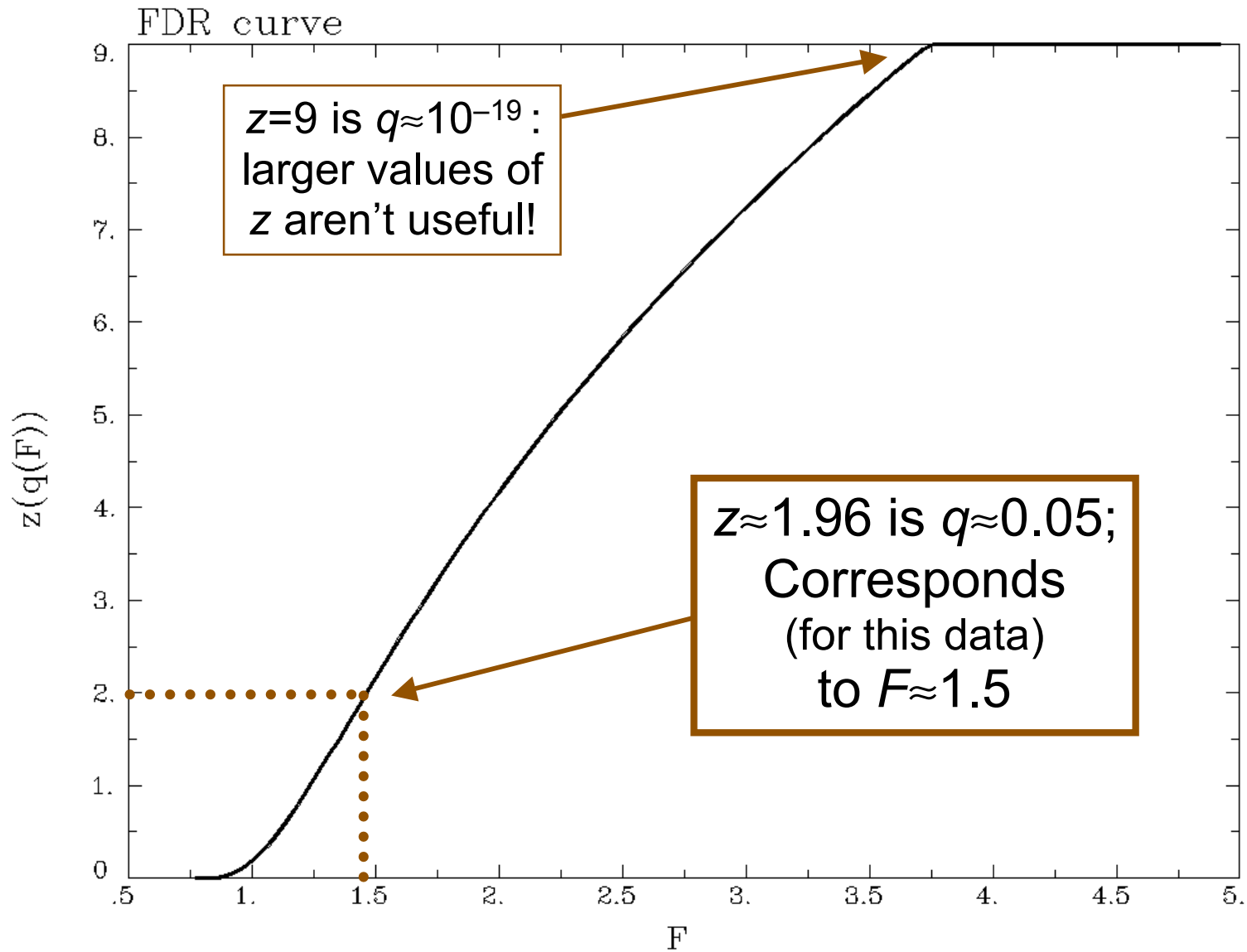
- Graph sorted p -values of voxel # k vs. $\kappa = k/N$ (the cumulative histogram of p , flipped sideways) and draw some lines from origin



Why This Line-Drawing Works



Same Data: threshold F vs. $z(q)$

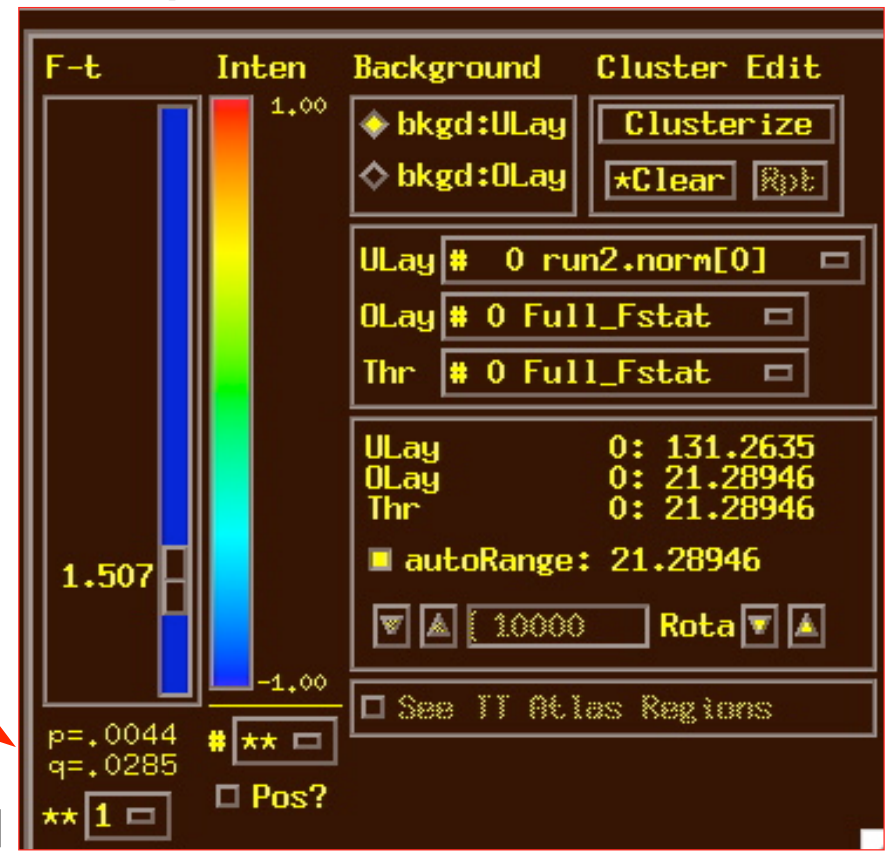


Recent Changes to 3dFDR

- Don't include voxels with $p=1$ (e.g., $F=0$), even if they are in the **-mask** supplied on the command line
 - This change decreases N , which will decrease q and so increase $z(q)$: recall that $q_{(k)} = \min_{m \geq k} [N \cdot P_{(m)} / m]$
- Sort with Quicksort algorithm
 - Faster than the bin-based sorting in the original code
 - Makes a big speed difference on large 1 mm³ datasets
 - Not much speed difference on small 3 mm³ grids, since there aren't so many voxels to sort
- Default mode of operation is '**-new**' method
 - Prints a warning message to let user know things have changed from the olden days
 - User can use '**-old**' method if desired

FDR curves: h vs. $z(q)$

- **3dDeconvolve**, **3dANOVAX**, **3dttest**, and **3dNLfim** now compute FDR curves for all statistical sub-bricks and store them in output header
 - **3drefit -addFDR** does same for other datasets
 - **3drefit -unFDR** can be used to delete such info
 - **AFNI** now shows p - and q -values below the threshold slider bar
 - Interpolates FDR curve from header (threshold $\rightarrow z \rightarrow q$)
 - Can be used to adjust threshold by “eyeball”
- $q = \text{N/A}$ means it's not available
- MDF hint = “missed detection fraction”



FDR Statistical Issues

- FDR is conservative (q -values are too large) when voxels are positively correlated (e.g., from spatially smoothing)
 - Correcting for this is not so easy, since q depends on data (including true positives), so a simulation like **AlphaSim** is hard to conceptualize
 - At present, FDR is an alternative way of controlling false positives, vs. **AlphaSim** (clustering)
 - Thinking about how to combine FDR and clustering
- Accuracy of FDR calculation depends on p -values being uniformly distributed under the null hypothesis
 - Statistic-to- p conversion should be accurate, which means that null F -distribution (say) should be correctly estimated
 - Serial correlation in FMRI time series means that **3dDeconvolve** denominator DOF is too large
 - \Rightarrow p -values will be too small, so q -values will be too small
 - **3dREMLfit** can ride to the rescue!

FWE or FDR?

- These 2 methods control Type I error in different sense
 - ★ FWE: $\alpha_{FW} = \text{Prob} (\geq \text{one false positive voxel/cluster in the whole brain})$
 - Frequentist's perspective: Probability among **many** hypothetical activation maps gathered under identical conditions
 - Advantage: can directly incorporate smoothness into estimate of α_{FW}
 - ★ FDR = expected fraction of false positive voxels among all detected voxels
 - Focus: controlling false positives among detected voxels in **one** activation map, as given by the experiment at hand
 - Advantage: not afraid of making a few Type I errors in a large field of true positives
 - ★ Concrete example
 - Individual voxel $p = 0.001$ for a brain of 25,000 EPI voxels
 - Uncorrected $\rightarrow \approx 25$ false positive voxels in the brain
 - FWE: corrected $p = 0.05 \rightarrow \approx 5\%$ of the time would expect one or more false positive clusters in the entire volume of interest
 - FDR: $q = 0.05 \rightarrow \approx 5\%$ of voxels among those **positively** labeled ones are false positive
- What if your favorite blob fails to survive correction?
 - ★ Tricks (don't tell anyone we told you about these)
 - One-tail t -test?
 - ROI-based statistics – e.g., grey matter mask, or whatever regions you focus on
 - ★ Analysis on surface; or, Use better group analysis tool (3dLME, 3dMEMA, etc.)

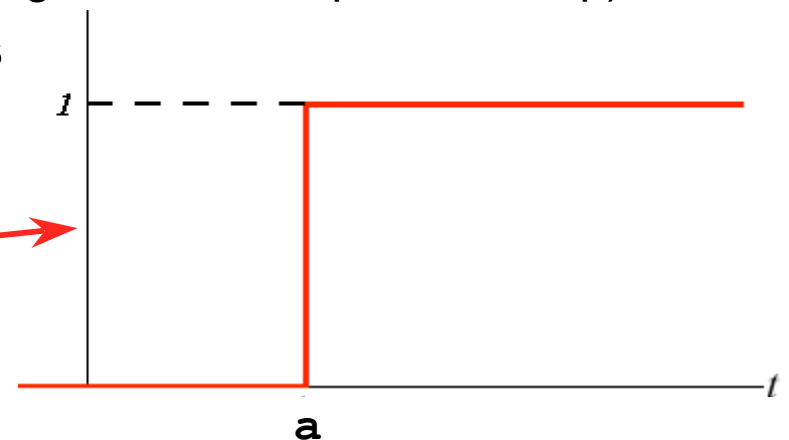
Conjunction Analysis

- **Conjunction**

- ★ Dictionary: “a compound proposition that is true if and only if all of its component propositions are true”
- ★ FMRI: areas that are active under 2 or more conditions (**AND** logic)
 - e.g, in a visual language task and in an auditory language task
- ★ Can also be used to mean analysis to find areas that are exclusively activated in one task but not another (**XOR** logic) or areas that are active in either task (non-exclusive **OR** logic)
- ★ If have n different tasks, have 2^n possible combinations of activation overlaps in each voxel (ranging from nothing there to complete overlap)

- ★ Tool: **3dcalc** applied to statistical maps

- Heaviside **step function** defines a *On/Off* logic
- $\text{step}(t-a) = 0$ if $t < a$
 $= 1$ if $t > a$
- Can be used to apply more than one threshold at a time



- Example of forming all possible conjunctions

- ★ 3 contrasts/tasks A, B, and C, each with a *t*-stat from **3dDeconvolve**

- ★ Assign each a number, based on binary positional notation:

 - A: $001_2 = 2^0 = 1$; B: $010_2 = 2^1 = 2$; C: $100_2 = 2^2 = 4$

- ★ Create a mask using 3 sub-bricks of *t* (e.g., threshold = 4.2)

```
3dcalc -a ContrA+tlrc -b ContrB+tlrc -c ContrC+tlrc \  
-expr '1*step(a-4.2)+2*step(b-4.2)+4*step(c-4.2)' \  
-prefix ConjAna
```

- ★ Interpret output, which has 8 possible ($=2^3$) scenarios:

 - 000₂ = **0**: none are active at this voxel

 - 001₂ = **1**: A is active, but no others

 - 010₂ = **2**: B, but no others

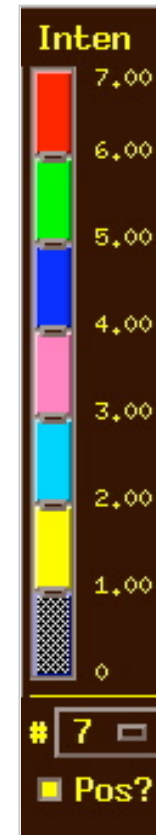
 - 011₂ = **3**: A and B, but not C

 - 100₂ = **4**: C but no others

 - 101₂ = **5**: A and C, but not B

 - 110₂ = **6**: B and C, but not A

 - 111₂ = **7**: A, B, and C are all active at this voxel



Can display each combination with a different color and so make pretty pictures that *might* even mean something!

- **Multiple testing correction issue**

- ★ How to calculate the p -value for the conjunction map?
- ★ No problem, *if* each entity was corrected (e.g., cluster-size thresholded at $t=4.2$) before conjunction analysis, via **AlphaSim**
- ★ But that may be too stringent (conservative) and over-corrected
- ★ With 2 or 3 entities, analytical calculation of conjunction p_{conj} is possible
 - Each individual test can have different uncorrected (per-voxel) p
 - Double or triple integral of tails of non-spherical (correlated) Gaussian distributions — not available in simple analytical formulae
- ★ With more than 3 entities, may have to resort to simulations
 - Monte Carlo simulations? (AKA: Buy a fast computer)
 - Will Gang Chen write such a program? Only time will tell!